# Cavanaugh Macdonald 

CONSULTING, LLC

The experience and dedication you deserve


Teachers Retirement System of Georgia Experience Investigation for the

Five-Year Period Ending June 30, 2018


# Cavanaugh Macdonald <br> C O N SULTIN G, LLC <br> The experience and dedication you deserve 

May 13, 2020
Board of Trustees
Teachers Retirement System of Georgia
Suite 100, Two Northside 75
Atlanta, GA 30318
Members of the Board:

We are pleased to submit the results of an investigation of the economic and demographic experience for the Teachers Retirement System of Georgia. The investigation has been made in accordance with Section 47-3-23(b) of the retirement law which provides that at least once in every five-year period, the actuary shall make an actuarial investigation into the mortality, service and compensation experience of the members and beneficiaries of the Retirement System. The purpose of the investigation is to assess the reasonability of the actuarial assumptions and methods currently used by the Retirement System. This investigation covers the five-year period from July 1, 2013 to June 30, 2018. As a result of this investigation, it is recommended that revised economic assumptions and demographic tables be adopted by the Board for future use.

The investigation of the demographic experience of members of the System includes all active and retired members as well as beneficiaries of deceased members. The experience was investigated separately for males and females where gender is a basis for material differences in experience.

The number of members expected to separate from active service, the expected rates of salary increase and the expected number of post-retirement deaths were obtained by use of the rates determined in the last experience investigation and adopted by the Board of Trustees. The results of the investigation indicate that the assumed rates of separation from active service due to withdrawal, disability, death and retirement and rates of post-retirement mortality need revision in order to provide a better fit between the actual and anticipated experience of the Retirement System. As a result of the investigation, new withdrawal, disability, retirement and mortality tables have been developed which reflect more closely the actual experience of the membership.

All new assumptions are shown in the attached tables in Appendix D of this report. In the actuary's judgment, the recommended assumptions are suitable for use until further experience indicates that modifications are desirable.

The experience investigation was performed by, and under the supervision of, independent actuaries who are members of the American Academy of Actuaries with experience in performing valuations for public retirement systems. John Garrett and Edward Koebel meet the Qualification Standards of the American Academy of Actuaries to render the actuarial opinion contained herein.

Respectfully submitted,


John Garrett, ASA, FCA, MAAA
Principal and Consulting Actuary
Cathy Turcot
Principal and Managing Director

Edward J. Koebel, FCA, EA, MAAA
Chief Executive Officer

Cavanaugh Macdonald
C O N SULTING, LLC
The experience and dedication you deserve

June 10, 2020
Dr. L. C. Evans
Executive Director
Teachers Retirement System of Georgia
Two Northside 75, Suite 100
Atlanta, GA 30318-7701

## Selection of Mortality Assumption in the Latest Experience Study

Dear Dr. Evans:
In the course of presenting the Experience Investigation Report for the Five-Year Period Ending July 1, 2018, a Board Member (Mr. Griffin) raised a question concerning our use of the headcountweighted rates versus the amount-weighted rates as the base mortality table in the assumption. We are writing to provide our reasoning for the mortality table selection.

There are two primary reasons we feel the headcount weighted table is appropriate for the selection of a reasonable mortality assumption to be used in the future valuations for the Teachers Retirement System (TRS). First, in our experience, large statewide teacher plans are homogenous groups and there are minor differences in amount-weighted experience. The Society of Actuaries (SOA) Pub-2010 Public Retirement Plans Mortality Table Report discusses the analysis utilized in developing both the amount-weighted and headcount-weighted mortality rates, and includes the following finding:

Broadly speaking, the difference between headcount-weighted and corresponding amountweighted annuity values represents a measure of the dispersion of individual amounts within the population being studied and the sensitivity of mortality to differences in income. More specifically, the larger the dispersion in underlying amounts, the greater (positive) differential between the amount-weighted annuity values relative to their headcountweighted counterparts. Therefore, the final columns in the three tables above indicate that

- The salary/benefit amount dispersion within the Teacher population (especially females) was considerably less than that for Safety and General and
- The salary/benefit amount dispersion for males is greater than that for females within all three job categories.

Dr. L. C. Evans
June 10, 2020
Page 2

As the TRS retired population is predominately female, we do not expect a material difference in the mortality experience based on amount weighting versus headcount weighting.

Second, the annual valuations determine the actuarial gains and losses on a benefit (or liability)weighted basis. Historically, the headcount-weighted tables which have been utilized in the past have consistently demonstrated a very close fit to experience. Future valuations will continue to assess the fit of the new mortality assumption on a benefit weighted measure though the annual actuarial gain/loss determinations.

The selection of a post-retirement mortality assumption is very material to the valuation results as it establishes the expected duration of all current and future annuity benefits provided by the Plan. The goal of the actuary is to recommend assumptions which minimize the future differences between actual and expected experience (on a liability basis) and results in the best estimate of the actuarial measures and funding requirements in the annual valuations. There is no advantage to favoring assumptions more conservative than experience. Conservative assumptions may lessen the potential of future losses but increase the potential for future gains resulting in the over-stating the true cost of the Plan and are at variance with the desire for long-term contribution stability.

The undersigned independent consulting actuary is a member of the American Academy of Actuaries. He has experience performing valuations and experience studies for large public retirement systems and is qualified to provide the opinions contained in this letter.

Please let me know if you have any questions.
Sincerely,


John J. Garrett, ASA, FCA, MAAA
Principal and Consulting Actuary
Attachment

## TABLE OF CONTENTS

Section Page
I Executive Summary ..... 1
II Financial Impact ..... 3
III Economic Assumptions ..... 4
IV Demographic Assumptions ..... 15
Rates of Withdrawal ..... 16
Rates of Disability Retirement ..... 22
Rates of Retirement ..... 25
Rates of Pre-Retirement Mortality ..... 30
Rates of Post-Retirement Mortality ..... 32
Rates of Salary Increase ..... 38
V Other Assumptions and Methods and Administrative Procedures ..... 39
Appendix
A Historical June CPI (U) Index ..... 40
B Capital Market Assumptions and Asset Allocation ..... 41
C Social Security Administration Wage Index ..... 42
D Recommended Rates ..... 43

## Section I <br> Executive Summary

The following table summarizes the findings and recommendations with regard to the assumptions utilized for the Teachers Retirement System of Georgia. Detailed explanations for the recommendations are found in the sections that follow.

| Summary of Recommended Economic and Demographic Assumptions |  |
| :--- | :--- |
|  | Economic Assumptions |$|$| Recommend no change in current assumption of 2.50\% |  |
| :--- | :--- |
| Inflation <br> Return | Composed of inflation assumption and real rate of return assumption. <br> We recommend no change in the current assumption of 7.25\%. |
| Real Rate of Wage <br> Increase | Recommend no change in the current assumption of 0.50\% annual <br> rate of real wage increases. |
| Payroll Growth Rate | Recommend no change in the current assumption of 3.00\%. |
|  | Recommend changes to current assumed rates of withdrawal that <br> overall increase the number of expected withdrawals. |
| Withdrawal | Recommend changes to current assumed rates of retirement that <br> overall increase the number of expected retirements. |
| Retirement | Recommend adoption of the Pub 2010 Teachers Headcount Weighted <br> Below Median mortality tables with ages set forward one year and <br> increased 6\%. Future improvement in mortality rates is assumed <br> using the adjusted MP-2019 projection scale generationally. |
| Mortality | Recommend lowering rates of expected disability retirement. |
| Disability | Recommend no change in current assumption. |

## Recommended Other Assumption and Method Changes

The table below lists the other assumptions and methods that are considered in our valuations that should be reviewed during the experience study.

| Assumption or Method | Recommended Change |
| :--- | :--- |
| Administrative Expenses | Recommend change to current assumption from $0.25 \%$ to <br> $0.20 \%$ of payroll |
| Amortization Method | No change to current method of level percent of payroll <br> amortization with annual layers of changes to UAAL |
| Asset Smoothing | No change to current method of smoothing market gains <br> and losses over 5 year period |
| Option Factors | Recommend change in current option factors to reflect <br> change in mortality rate |
| Percent Married | Recommend no change to current assumption |
| Unused Sick Leave | Recommend changes to our loads on service for allowing <br> members to convert forfeited sick leave to service at <br> retirement |
| Valuation Cost Method | No change in Entry Age Normal Cost Method |
| Vested Termination Benefit | Recommend change to current assumption |

## Section II Financial Impact

The following table highlights the impact of the recommended changes on the principal valuation results. This table is for illustrative purposes only and not intended to modify the contribution rates set forth in the June 30, 2018 valuation report.

| Impact on Principal Valuation Results (\$1,000's) |  |  |
| :---: | :---: | :---: |
|  | Valuation Results 2018 | Recommended Assumptions |
| Unfunded Accrued Liability | \$21,880,889 | \$22,962,411 |
| Funding Ratio | 77.4\% | 76.6\% |
| Employer Annual Required Contribution |  |  |
| Normal Rate* | 7.25\% | 7.40\% |
| Unfunded Accrued Liability Rate | $\underline{11.81 \%}$ | 12.35\% |
| Total Rate | 19.06\% | 19.75\% |
| Amortization Period (in years) | 25.6 | 25.8 |

## Section III

## Economic Assumptions

There are three economic assumptions used in the actuarial valuations performed for the System. They are:

- Price Inflation
- Investment Return
- Wage Inflation

Actuarial Standard of Practice (ASOP) No. 27, "Selection of Economic Assumptions for Measuring Pension Obligations", provides guidance to actuaries in selecting economic assumptions for measuring obligations under defined benefit plans and was revised in September 2013. The revised standard now requires that each economic assumption selected by the actuary should be reasonable which means it has the following characteristics:

- It is appropriate for the purpose of the measurement;
- It reflects the actuary's professional judgment;
- It takes into account historical and current economic data that is relevant as of the measurement date;
- It reflects the actuary's estimate of future experience, the actuary's observation of the estimates inherent in market data, or a combination thereof; and
- It has no significant bias (i.e., it is not significantly optimistic or pessimistic), except when provisions for adverse deviation or plan provisions that are difficult to measure are included and disclosed, or when alternative assumptions are used for the assessment of risk.

Each economic assumption should individually satisfy this standard. Furthermore, with respect to any particular valuation, each economic assumption should be consistent with every other economic assumption over the measurement period.

In conjunction with the June 30, 2018 valuation we reviewed the System's economic assumptions and recommended changes. Those changes were adopted by the Board on May 15, 2019. We have updated our analysis of the System's economic assumptions but recommend no further revisions at this time.

In our opinion, the economic assumptions recommended in this report have been developed in accordance with ASOP No. 27, as revised in September, 2013. The following table shows our recommendation followed by detailed discussions of each assumption.

| Item | Current | Proposed |
| :--- | :--- | :---: |
| Price Inflation | $2.50 \%$ | $2.50 \%$ |
| Real Rate of Return | $\underline{4.75}$ | $\underline{4.75}$ |
| Investment Return | $7.25 \%$ | $7.25 \%$ |
| Price Inflation | $2.50 \%$ |  |
| Real Wage Growth | $\underline{0.50 \%}$ | $2.50 \%$ |
| Wage Inflation | $3.00 \%$ | $\underline{0.50 \%}$ |

## Price Inflation

Background: Assumed price inflation is used as the basis for both the investment return assumption and the wage inflation assumption. These latter two assumptions will be discussed in detail in the following sections.

It is important that the price inflation assumption be consistently applied throughout the economic assumptions utilized in an actuarial valuation. This is called for in ASOP No. 27 and is also required to meet the parameters for determining pension liabilities and expenses under Governmental Accounting Standards Board (GASB) Statements No. 67 and 68.

The current price inflation assumption is $2.50 \%$ per year.
Past Experience: The Consumer Price Index, US City Average, All Urban Consumers, CPI (U), has been used as the basis for reviewing historical levels of price inflation. The level of that index in June of each of the last 50 years is provided in Appendix A.

In analyzing this data, annual rates of inflation have been determined by measuring the compound growth rate of the $\mathrm{CPI}(\mathrm{U})$ over various time periods. The results are as follows:

| Period <br> (Fiscal Years <br> Ending) | Number of <br> Years | Inflation | Annual <br> Standard Deviation |
| :---: | :---: | :---: | :---: |
| $2009-2018$ | 10 | $1.42 \%$ | $1.39 \%$ |
| $1999-2008$ | 10 | 2.99 | 1.17 |
| $1989-1998$ | 10 | 3.28 | 1.16 |
| $1979-1988$ | 10 | 6.11 | 4.15 |
| $1969-1978$ | 10 | 6.51 | 2.31 |
| $1999-2018$ | 20 | $2.20 \%$ |  |
| $1989-2018$ | 30 | 2.56 | $1.49 \%$ |
| $1979-2018$ | 40 | 3.44 | 1.46 |
| $1969-2018$ | 50 | 4.04 | 2.84 |
| $1927-2018$ | 92 | 2.91 | 2.99 |

The graph below shows the annual increases in the CPI (U) over the 50-year period (1969-2018) compared to the $2.50 \%$ currently assumed.


Over shorter historical periods, the average annual rate of increase in the CPI-U has been below $3.00 \%$. The period of high inflation from 1973 to 1982 has a significant impact on the averages over periods which include these rates. Further, the average rate of $2.91 \%$ over the entire 92 -year period is higher than the average rate of $2.56 \%$ for the prior 30 years ( 1989 to 2018) but, more importantly, the volatility of the annual rates in the more recent years has been markedly lower as indicated by the significantly lower annual standard deviations. Many experts attribute the lower average annual rates and lower volatility to the increased efforts of the Federal Reserve since the early 1980's to stabilize price inflation. In our judgement, the post-1981 period of inflation is a more meaningful representation of historical price inflation than longer-term measures. The severe recession of 2007-2009 resulted in a short period of deflation followed by low levels of inflation. Although the quantitative easing program has ended, the Federal Reserve has disclosed an inflation target of $2.0 \%$ which has been higher than the post-recession average rate of inflation of $1.74 \%$ as measured from the CPI-U by fiscal years.

The bond market's measure of expected inflation is shown by the spread between the nominal yield on U.S. government bonds and Treasury Inflation Protected Securities (TIPS) of the same maturity. As of June 30, 2018, the spread at 10, 20 and 30 year maturities were all around $2.10 \%$ which is called the breakeven rate of inflation.

Recommendation: Although the 10 -year average price inflation rate of $1.42 \%$ is significantly lower than the System's assumed rate of $2.50 \%$, the longer 30 -year average rate of $2.56 \%$ is slightly higher than the System's assumed rate. We rely more heavily on longer-term historical data and note that both the Fed's inflation target and the Bond market's expectation are higher than the short-term historical rates.

An additional reliable source of expected rates of inflation, the 2019 OASDI Trustees Report, the Chief Actuary for Social Security bases the 75-year cost projections on an intermediate inflation assumption of $2.6 \%$ with a range from $2.0 \%$ to $3.2 \%$. We consider that range to be reasonable and recommend that TRS maintains the current price inflation rate assumption of $2.50 \%$.


## Investment Rate of Return

Background: The assumed investment return is one of the most significant assumptions in the annual actuarial valuation process as it is used to discount the expected benefit payments for all active, inactive and retired members of the System. Minor changes in this assumption can have a major impact on valuation results. The investment return assumption should reflect the asset allocation target for the funds set by the Board of Trustees.

The current assumption is $7.25 \%$, consisting of a price inflation assumption of $2.50 \%$ and a real rate of return assumption of $4.75 \%$. The return is net of investment expenses.

Past Experience: The assets for the System are valued using a widely accepted asset-smoothing methodology (5-year smoothing) that fully recognizes the expected investment income and also recognizes $20 \%$ of each year's investment gain or loss (the difference between actual and expected investment income). The asset smoothing methodology from 2010 to 2012 was based on 7-year smoothing and actuarial value was set equal to market value in 2013. The recent experience over the last five years is shown in the table below.

| Year <br> Ending <br> $\mathbf{6 / 3 0}$ | Actuarial Value | Market Value |
| :---: | :---: | :---: |
| 2014 | 9.41 | 17.17 |
| 2015 | 9.02 | 3.70 |
| 2016 | 7.30 | 1.40 |
| 2017 | 7.80 | 12.50 |
| 2018 | 8.36 | 8.95 |
| Average | $8.40 \%$ | $8.60 \%$ |

The impact of the asset smoothing method can be observed in the table. Although the average returns over the five-year period are very close, the return on actuarial value is, as expected, less variable. We also note, as provided by the guidance of the Actuarial Standards of Practice (ASOP), that historical returns over a short time period are not credible for the purpose of setting the longterm assumed future rate of return.

We next include in our analysis information concerning future expectations for the investment return assumption. We prefer to base our investment return assumption largely on the capital market assumptions utilized by the Board in setting investment policy and the System's asset allocation. The investment rate of return assumption has two component parts: the rate of price inflation and the real rate of investment return. This component approach is referred to as the building block method in ASOP No. 27. The price inflation component was discussed previously in this report, therefore, this section will focus on the real rate of investment return component.

Analysis: The current capital market assumptions and asset allocation as provided by the System investment staff are shown in Appendix B. We further assumed that investment returns approximately follow a lognormal distribution with no correlation between years. The results below provide an expected range of real rates of return over up to a 50 -year time horizon. Looking at one year results produces an expected real return of $6.4 \%$ but also has a high standard deviation or measurement of volatility. By expanding the time horizon, the compound average return approaches the expected median of future real returns and the volatility declines significantly. The following table provides a summary of results. The geometric real rates of return are net of investment expenses.

| Time <br> Span <br> In <br> Years | Mean <br> Real <br> Return | Standard <br> Deviation | $\mathbf{5}^{\text {th }}$ |  |  |  |  |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |

Based on this analysis the median ( $50^{\text {th }}$ percentile) real rate of return over a 50 -year period is $5.5 \%$. It can also be anticipated that for the 10 -year time span, $50 \%$ of the expected compound average real rates of return were between $2.7 \% \%$ and $8.4 \%$. As the time span increases, this spread begins to narrow. Over a 50-year time span, the analysis indicates there is a $25 \%$ likelihood that real returns will average below $4.2 \%$ and a $25 \%$ likelihood they will be above $6.8 \%$. In other words, $50 \%$ of the distribution of expected compound average real returns will be between $4.2 \%$ and $6.8 \%$.

Using the building block approach of ASOP No. 27 and the projection results outlined above, we have determined a range for the investment return assumption of the $25^{\text {th }}$ to $75^{\text {th }}$ percentile real returns over the 50 -year time span plus the recommended inflation assumption. The following table details the range.

| Item | $\mathbf{2 5}^{\text {th }}$ Percentile | $\mathbf{5 0}^{\text {th }}$ Percentile | $\mathbf{7 5}^{\text {th }}$ Percentile |
| :--- | :--- | :---: | :--- |
| Real Rate of Return* | $4.20 \%$ | $5.50 \%$ | $6.80 \%$ |
| Inflation | $\underline{2.50}$ | $\underline{2.50}$ | $\underline{2.50}$ |
| Net Investment Return | $6.70 \%$ | $8.00 \%$ | $\mathbf{9 . 3 0 \%}$ |

* net of investment expenses

Based on the capital market assumptions provided by the System's investment experts, the median expected compound average return is $8.0 \%$ over a 50 -year period. The current $7.25 \%$ assumed rate of return is approximately the 35th percentile of the distribution of expected average rate of returns over a 50 -year period. Although not in the center of the recommended range, in our opinion a return of $7.25 \%$ is a reasonable expectation with a sufficient margin to account for adverse experience. It should be noted that the capital market assumptions of investment professionals will vary from year to year and can differ substantially from investment professional to investment professional. Different market expectations could impact the development of a recommended assumptions.

For a broader view of expected returns, we also reviewed the 2018 Survey of Capital Market Assumptions produced by Horizon Actuarial Services, LLC to see what other investment professionals are currently using for capital market assumptions. The Horizon survey includes both 10-year horizon and 20-year horizon capital market assumptions of several investment consultants. Using the Board's current target asset allocation, we applied the same statistical analysis to these survey results as we did the capital market assumption of the investment staff with the following results for the 20-year horizon:

| Time <br> Span <br> In <br> Years | Mean <br> Real <br> Return | Standard <br> Deviation | $\mathbf{5}^{\text {th }}$ | $\mathbf{2 5}^{\text {th }}$ | $\mathbf{5 0}^{\text {th }}$ | $\mathbf{7 5}^{\text {th }}$ | $\mathbf{9 5}^{\text {th }}$ |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | $5.2 \%$ | $12.0 \%$ | $-13.3 \%$ | $-3.2 \%$ | $4.5 \%$ | $12.8 \%$ | $25.9 \%$ |
| 5 | $4.6 \%$ | $5.3 \%$ | $-3.9 \%$ | $1.0 \%$ | $4.5 \%$ | $8.1 \%$ | $13.6 \%$ |
| 10 | $4.5 \%$ | $3.8 \%$ | $-1.5 \%$ | $2.0 \%$ | $4.5 \%$ | $7.0 \%$ | $10.8 \%$ |
| 20 | $4.5 \%$ | $2.7 \%$ | $0.2 \%$ | $2.7 \%$ | $4.5 \%$ | $6.3 \%$ | $8.9 \%$ |
| 30 | $4.5 \%$ | $2.2 \%$ | $1.0 \%$ | $3.0 \%$ | $4.5 \%$ | $5.9 \%$ | $8.1 \%$ |
| 50 | $4.5 \%$ | $1.7 \%$ | $1.8 \%$ | $3.4 \%$ | $4.5 \%$ | $5.6 \%$ | $7.3 \%$ |

Again, using the building block approach and the Horizon projection results, the following shows the range for the investment return assumptions.

| Item | $\mathbf{2 5}^{\text {th }}$ Percentile | $\mathbf{5 0}^{\text {th }}$ Percentile | $\mathbf{7 5}^{\text {th }}$ Percentile |
| :--- | :--- | :---: | :--- |
| Real Rate of Return | $3.35 \%$ | $4.47 \%$ | $5.61 \%$ |
| Inflation | $\underline{2.50}$ | $\underline{2.50}$ | $\underline{2.50}$ |
| Net Investment Return | $5.85 \%$ | $6.97 \%$ | $8.11 \%$ |

Using this basis, the $7.25 \%$ is slightly above the median expected return over a 50 -year period. We prefer the use of the capital market assumptions of the Board's investment professionals over the assumptions from a survey of several consultants which do not serve the Board since the survey assumptions were not the basis for the asset allocation decisions of the Board. By the guidance of the actuarial standards, we maintain a long-term perspective in setting all assumptions, especially the investment return assumption.

In the course of constructing an investment return assumption, while we don't develop the recommended investment rate of return based on those used by your peers, we also consider the range of assumptions used by other large public retirement systems. The graph below is from a recent Public Fund Survey, note that the current median return assumptions for the approximately 125 large public plans in the survey is $7.25 \%$. Further, note that the trend in the return assumptions of these large plans is toward lower assumed rates of return.


Recommendation: We are recommending that the long-term investment return assumption remain at $7.25 \%$.

| Investment Return Assumption |  |  |
| :--- | :--- | :---: |
|  | Current | Recommended |
| Real Rate of Return* | $4.75 \%$ | $4.75 \%$ |
| Inflation | $\underline{2.50}$ | $\underline{2.50}$ |
| Net Investment Return | $7.25 \%$ | $7.25 \%$ |

* net of investment expenses


## Wage Inflation

Background: The assumed future increases in salaries consist of a wage inflation component and a component for promotion and longevity, often called merit increases. Wage inflation normally consists of price inflation and a component for real wage growth which reflects the overall return on labor in the economy. Merit increases are generally age and or service related, and will be discussed in the demographic assumption section of the report.

The current wage inflation assumption is $3.00 \%$ and is composed of a $2.50 \%$ rate of inflation assumption and a $0.50 \%$ real rate of wage inflation.

Past Experience: The Social Security Administration publishes data on wage growth in the United States. Appendix C shows the last 50 calendar years' data. We provide the rates of wage inflation and a comparison with the rates of price inflation over various calendar year time periods in the table below. We remove the rate of price inflation for each calendar year for the data to result in the historical real rate of wage inflation.

| Period <br> (Calendar Years <br> Ending) | Number <br> of Years | Wage Inflation | Price Inflation | Real Wage <br> Growth |
| :---: | :---: | :---: | :---: | :---: |
| $2009-2018$ | 10 | $2.35 \%$ | $1.80 \%$ | $0.55 \%$ |
| $1999-2008$ | 10 | 3.66 | 2.52 | 0.84 |
| $1989-1998$ | 10 | 4.09 | 3.12 | 0.97 |
| $1979-1988$ | 10 | 6.24 | 5.94 | 0.30 |
| $1969-1978$ | 10 | 6.60 | 6.67 | $(0.07)$ |
| $1999-2018$ | 20 | $3.00 \%$ | $2.16 \%$ | $0.84 \%$ |
| $1989-2018$ | 30 | 3.36 | 2.48 | 0.88 |
| $1979-2018$ | 40 | 4.07 | 3.33 | 0.74 |
| $1969-2018$ | 50 | 4.57 | 3.99 | 0.58 |

As the analysis of the national wage growth data shows, the shorter-term historical average real rate of wage inflation ( $0.55 \%$ for latest 10 year period) is slightly less than the longer-term average real rate ( $0.58 \%$ over 50 years). The rate of real wage inflation over the prior 20 and 30 year periods is $0.84 \%$ and $0.88 \%$ respectively.

The apparent annual real wage growth rate experience of TRS during the experience study period averaged a $1.07 \%$ above inflation compared to the real growth in the national average wages of $1.53 \%$. The 5 -year historical period is not materially relevant for setting this assumption but it is important that the System's experienced lower rates of increase than reflected nationally.

Recommendation: Based on the apparent real wage growth from the actual wage data and consistent with the longer term real growth in the national average wage data, we recommend no change to the current assumed rate of real wage growth of $0.50 \%$ per year.

| Wage Inflation Assumption |  |  |
| :--- | :---: | :---: |
|  | Current | Recommended |
| Price Inflation | $2.50 \%$ | $2.50 \%$ |
| Real Wage Growth | $\underline{0.50}$ | $\underline{0.50}$ |
| Wage Inflation | $3.00 \%$ | $3.00 \%$ |

Payroll Growth Assumption: The current amortization method is level percent of payroll which requires the use of an assumed rate of annual payroll growth. This assumption typically ranges from the rate of inflation ( $2.50 \%$ ) to the rate of wage inflation (3.00\%). We recommend continued use of the current $3.00 \%$ payroll growth assumption.

## Section IV

Demographic Assumptions
There are several demographic assumptions used in the actuarial valuations performed for the Teachers Retirement System of Georgia. They are:

- Rates of Withdrawal
- Rates of Disability Retirement
- Rates of Service Retirement
- Rate of Mortality
- Rates of Salary Increase

The Actuarial Standards Board has issued Actuarial Standard of Practice (ASOP) No. 35, "Selection of Demographic and Other Noneconomic Assumptions for Measuring Pension Obligations", which provides guidance to actuaries in selecting demographic assumptions for measuring obligations under defined benefit plans. In our opinion, the demographic assumptions recommended in this report have been developed in accordance with ASOP No. 35.

The purpose of a study of demographic experience is to compare what actually happened to the membership during the study period (July 1, 2013, through June 30, 2018) with what was expected to happen based on the assumptions used in the last five actuarial valuations.

Detailed tabulations by age, service and/or gender are performed over the entire study period. These tabulations look at all active and retired members during the period as well as separately annotating those who experience a demographic event, also referred to as a decrement. In addition the tabulation of all members together with the current assumptions permits the calculation of the number of expected decrements during the study period.

If the actual experience differs significantly from the overall expected results, or if the pattern of actual decrements, or rates of decrement, by age, gender, or service does not follow the expected pattern, new assumptions are recommended. Recommended changes usually do not follow the exact actual experience during the observation period. Judgment is required to extrapolate future experience from past trends and current member behavior.

The remainder of this section presents the results of the demographic study. We have prepared tables that show a comparison of the actual and expected decrements and the overall ratio of actual to expected results (A/E Ratios) under the current assumptions. If a change is being proposed, the revised A/E Ratios are shown as well. Salary adjustments, other than the economic assumption for wage inflation discussed in the previous section, are treated as demographic assumptions.

## RATES OF WITHDRAWAL

## COMPARISON OF ACTUAL AND EXPECTED WITHDRAWALS FROM ACTIVE SERVICE

| CENTRAL <br> AGE <br> OF GROUP | NUMIBER OF WITHIDRAWALS |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | MALE |  |  | FEMALE |  |  |
|  | Actual | Expected | Ratio of Actual to Expected | Actual | Expected | Ratio of Actual to Expected |
|  | Withdrawals with less than 5 years of service |  |  |  |  |  |
| 20 | 130 | 114.8 | 1.132 | 219 | 205.0 | 1.068 |
| 25 | 2,000 | 1,868.1 | 1.071 | 5,657 | 5,769.5 | 0.981 |
| 30 | 2,157 | 2,047.7 | 1.053 | 5,867 | 5,797.6 | 1.012 |
| 35 | 1,580 | 1,437.8 | 1.099 | 3,956 | 3,885.7 | 1.018 |
| 40 | 1,132 | 1,107.5 | 1.022 | 3,331 | 3,063.0 | 1.087 |
| 45 | 1,006 | 933.1 | 1.078 | 2,904 | 2,724.8 | 1.066 |
| 50 | 742 | 703.6 | 1.055 | 2,112 | 1,914.3 | 1.103 |
| 53 \& Over | 1,331 | 1,138.3 | 1.169 | 2,940 | 2,437.9 | 1.206 |
| TOTAL | 10,078 | 9,350.9 | 1.078 | 26,986 | 25,797.8 | 1.046 |
|  | Withdrawals with at least 5 but less than 10 years of service |  |  |  |  |  |
| 25 | 48 | 40.1 | 1.197 | 92 | 146.2 | 0.629 |
| 30 | 664 | 668.3 | 0.994 | 2,673 | 2,876.4 | 0.929 |
| 35 | 760 | 724.6 | 1.049 | 2,431 | 2,383.1 | 1.020 |
| 40 | 562 | 510.8 | 1.100 | 1,771 | 1,722.5 | 1.028 |
| 45 | 454 | 445.0 | 1.020 | 1,648 | 1,618.6 | 1.018 |
| 50 | 357 | 334.3 | 1.068 | 1,325 | 1,247.2 | 1.062 |
| 53 \& Over | 813 | 681.2 | 1.193 | 2,006 | 1,849.8 | 1.084 |
| TOTAL | 3,658 | 3,404.3 | 1.075 | 11,946 | 11,843.8 | 1.009 |
|  | Withdrawals with 10 or greater years of service |  |  |  |  |  |
| 30 | 18 | 22.5 | 0.800 | 60 | 63.7 | 0.942 |
| 35 | 330 | 275.4 | 1.198 | 1,547 | 1,258.2 | 1.230 |
| 40 | 541 | 465.5 | 1.162 | 1,931 | 1,578.4 | 1.223 |
| 45 | 595 | 508.6 | 1.170 | 2,117 | 1,814.8 | 1.167 |
| 50 | 492 | 418.8 | 1.175 | 2,050 | 1,566.5 | 1.309 |
| 53 \& Over | 632 | 537.2 | 1.176 | 2,783 | 2,278.3 | 1.222 |
| TOTAL | 2,608 | 2,228.0 | 1.171 | 10,488 | 8,559.9 | 1.225 |

The following graphs show a comparison of the current expected, actual, and proposed rates of withdrawal for actives.




Withdrawal Rates (SVC 5-9) - Females


Page 18



The rates of withdrawal adopted by the Board are used to determine the expected number of separations from active service which will occur as a result of resignation or dismissal. The preceding results indicate that during the study period more members than expected withdrew in all service categories for both males and females except at some of the younger ages. More withdrawals than expected create gains to the System since fewer members remain in service to accrue additional benefits. We recommend that the rates of withdrawal be revised at this time to more closely reflect the experience of the System.

## COMPARATIVE RATES OF WITHDRAWAL FROM ACTIVE SERVICE

| AGE | RATES OF WITHIDRAWAL |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Present |  |  | Proposed |  |  |
|  | Years Of Service |  |  | Years Of Service |  |  |
|  | 0-4 | 5-9 | 10 + | 0-4 | 5-9 | 10 + |
|  | Male |  |  |  |  |  |
| 20 | 25.00\% |  |  | 27.00\% |  |  |
| 25 | 17.00\% | 12.00\% |  | 17.00\% | 13.00\% |  |
| 30 | 13.50\% | 7.00\% | 8.00\% | 14.00\% | 6.50\% | 6.00\% |
| 35 | 13.50\% | 6.00\% | 3.00\% | 14.00\% | 6.25\% | 3.50\% |
| 40 | 13.00\% | 6.00\% | 2.50\% | 13.00\% | 6.25\% | 2.75\% |
| 45 | 12.00\% | 6.00\% | 2.30\% | 13.00\% | 6.00\% | 2.50\% |
| 50 | 11.00\% | 5.50\% | 2.50\% | 11.25\% | 5.75\% | 2.75\% |
| 55 | 11.00\% | 5.50\% | 3.00\% | 11.75\% | 5.50\% | 3.25\% |
| 60 | 12.00\% | 5.50\% | 0.00\% | 12.00\% | 6.00\% | 0.00\% |
| 64 | 13.00\% | 6.50\% | 0.00\% | 15.00\% | 7.50\% | 0.00\% |
|  | Female |  |  |  |  |  |
| 20 | 28.00\% |  |  | 28.00\% |  |  |
| 25 | 13.50\% | 16.00\% |  | 13.50\% | 12.00\% |  |
| 30 | 13.50\% | 8.00\% | 6.00\% | 13.50\% | 7.00\% | 6.00\% |
| 35 | 13.00\% | 7.00\% | 3.50\% | 13.00\% | 7.00\% | 4.00\% |
| 40 | 11.00\% | 6.50\% | 3.00\% | 12.00\% | 6.50\% | 3.00\% |
| 45 | 10.50\% | 6.00\% | 2.30\% | 10.75\% | 6.00\% | 2.50\% |
| 50 | 10.00\% | 5.00\% | 2.40\% | 10.75\% | 5.50\% | 3.00\% |
| 55 | 10.00\% | 5.00\% | 2.75\% | 10.75\% | 5.00\% | 3.00\% |
| 60 | 10.50\% | 5.50\% | 0.00\% | 11.50\% | 5.50\% | 0.00\% |
| 64 | 13.00\% | 6.50\% | 0.00\% | 15.00\% | 7.50\% | 0.00\% |

## COMPARISON OF ACTUAL AND EXPECTED WITHDRAWALS BASED ON PROPOSED RATES

| $\begin{aligned} & \text { CENTRAL } \\ & \text { AGE } \\ & \text { OF GROUP } \end{aligned}$ | NUMBER OF WITHIDRAWALS |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | MALE |  |  | FEMALE |  |  |
|  | Actual | Expected | Ratio of Actual to Expected | Actual | Expected | Ratio of Actual to Expected |
|  | Withdrawals with less than 5 years of service |  |  |  |  |  |
| 20 | 130 | 123.9 | 1.049 | 219 | 205.0 | 1.068 |
| 25 | 2,000 | 1,960.2 | 1.020 | 5,657 | 5,769.5 | 0.981 |
| 30 | 2,157 | 2,123.5 | 1.016 | 5,867 | 5,797.6 | 1.012 |
| 35 | 1,580 | 1,491.0 | 1.060 | 3,956 | 3,885.7 | 1.018 |
| 40 | 1,132 | 1,107.5 | 1.022 | 3,331 | 3,169.5 | 1.051 |
| 45 | 1,006 | 977.7 | 1.029 | 2,904 | 2,803.0 | 1.036 |
| 50 | 742 | 719.6 | 1.031 | 2,112 | 2,057.9 | 1.026 |
| 53 \& Over | 1,331 | 1,224.7 | 1.087 | 2,940 | 2,664.5 | 1.103 |
| TOTAL | 10,078 | 9,728.1 | 1.036 | 26,986 | 26,352.7 | 1.024 |
|  | Withdrawals with at least 5 but less than 10 years of service |  |  |  |  |  |
| 25 | 48 | 43.4 | 1.106 | 92 | 109.7 | 0.839 |
| 30 | 664 | 660.5 | 1.005 | 2,673 | 2,708.9 | 0.987 |
| 35 | 760 | 754.8 | 1.007 | 2,431 | 2,383.1 | 1.020 |
| 40 | 562 | 532.1 | 1.056 | 1,771 | 1,722.5 | 1.028 |
| 45 | 454 | 445.0 | 1.020 | 1,648 | 1,618.6 | 1.018 |
| 50 | 357 | 343.5 | 1.039 | 1,325 | 1,271.2 | 1.042 |
| 53 \& Over | 813 | 733.0 | 1.109 | 2,006 | 1,891.0 | 1.061 |
| TOTAL | 3,658 | 3,512.3 | 1.041 | 11,946 | 11,705.0 | 1.021 |
|  | Withdrawals with $\mathbf{1 0}$ or greater years of service |  |  |  |  |  |
| 30 | 18 | 19.0 | 0.947 | 60 | 59.1 | 1.015 |
| 35 | 330 | 317.2 | 1.040 | 1,547 | 1,488.6 | 1.039 |
| 40 | 541 | 508.9 | 1.063 | 1,931 | 1,847.9 | 1.045 |
| 45 | 595 | 563.3 | 1.056 | 2,117 | 2,023.1 | 1.046 |
| 50 | 492 | 467.8 | 1.052 | 2,050 | 1,960.4 | 1.046 |
| 53 \& Over | 632 | 606.2 | 1.043 | 2,783 | 2,485.4 | 1.120 |
| TOTAL | 2,608 | 2,482.4 | 1.051 | 10,488 | 9,864.5 | 1.063 |

## RATES OF DISABILITY RETIREMENT

## COMPARISON OF ACTUAL AND EXPECTED DISABILITY RETIREMENTS

| $\begin{aligned} & \text { CENTRAL } \\ & \text { AGE } \\ & \text { GROUP } \end{aligned}$ | NUMBER OF DISABILITY RETIREMIENTS |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | MALE |  |  | FEMALE |  |  |
|  | Actual | Expected | Ratio of Actual to Expected | Actual | Expected | Ratio of Actual to Expected |
| 27 \& Under | 0 | 1.7 | 0.000 | 0 | 5.7 | 0.000 |
| 30 | 0 | 5.2 | 0.000 | 0 | 11.7 | 0.000 |
| 35 | 2 | 10.6 | 0.189 | 10 | 19.3 | 0.518 |
| 40 | 9 | 19.0 | 0.474 | 34 | 43.3 | 0.785 |
| 45 | 28 | 33.5 | 0.836 | 88 | 90.8 | 0.969 |
| 50 | 40 | 59.5 | 0.672 | 177 | 195.9 | 0.904 |
| 53 \& Over | 109 | 127.6 | 0.854 | 486 | 570.6 | 0.852 |
| TOTAL | 188 | 257.1 | 0.731 | 795 | 937.3 | 0.848 |

The following graphs show a comparison of the current expected, actual, and proposed rates of disability retirement.



During the period under investigation, the actual rates of disability retirement were less than expected in all age groups. We recommend the rates of disability retirement be revised to reflect the experience of the System. The following table shows a comparison between the present disability retirement rates and the proposed rates.

## COMPARATIVE RATES OF DISABILITY RETIREMENTS

| AGE | RATES OF DISABILITY |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | MALE |  | FEMALE |  |
|  | Present | Proposed | Present | Proposed |
| 25 | 0.0135\% | 0.0000\% | 0.0130\% | 0.0000\% |
| 30 | 0.0210\% | 0.0000\% | 0.0140\% | 0.0000\% |
| 35 | 0.0330\% | 0.0165\% | 0.0190\% | 0.0152\% |
| 40 | 0.0550\% | 0.0275\% | 0.0390\% | 0.0312\% |
| 45 | 0.0900\% | 0.0720\% | 0.0650\% | 0.0650\% |
| 50 | 0.1700\% | 0.1360\% | 0.1400\% | 0.1400\% |
| 55 | 0.3000\% | 0.2400\% | 0.3400\% | 0.3400\% |

## COMPARISON OF ACTUAL AND EXPECTED DISABILITY RETIREMENTS BASED ON PROPOSED RATES

| $\begin{aligned} & \text { CENTRAL } \\ & \text { AGE } \\ & \text { OF GROUP } \end{aligned}$ | NUMBER OF DISABILITY RETIRIDMINTS |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | MALE |  |  | FEMALE |  |  |
|  | Actual | Expected | Ratio of Actual to Expected | Actual | Expected | Ratio of Actual to Expected |
| 27 \& Under | 0 | 0.0 | 0.000 | 0 | 0.0 | 0.000 |
| 30 | 0 | 0.0 | 0.000 | 0 | 0.0 | 0.000 |
| 35 | 2 | 5.3 | 0.377 | 10 | 15.4 | 0.649 |
| 40 | 9 | 9.5 | 0.947 | 34 | 34.6 | 0.983 |
| 45 | 28 | 26.8 | 1.045 | 88 | 90.8 | 0.969 |
| 50 | 40 | 47.6 | 0.840 | 177 | 195.9 | 0.904 |
| $53 \&$ Over | 109 | 102.1 | 1.068 | 486 | 570.6 | 0.852 |
| TOTAL | 188 | 191.3 | 0.983 | 795 | 907.3 | 0.876 |

## RATES OF RETIREMENT

## COMPARISON OF ACTUAL AND EXPECTED RETIREMENTS

| $\begin{gathered} \text { CENTRAL } \\ \text { AGE } \\ \text { OF GROUP } \end{gathered}$ | NUMBER OF SERVICE RETIREMIENTS |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | MALE |  |  | FEMALE |  |  |
|  | Actual | Expected | Ratio of Actual to Expected | Actual | Expected | Ratio of Actual to Expected |
| 49 \& Under 52 | Less than 30 years of service or all ages 65 and over |  |  |  |  |  |
|  | 18 | 39.4 | 0.457 | 98 | 166.4 | 0.589 |
|  | 124 | 163.9 | 0.757 | 446 | 514.8 | 0.866 |
| 57 | 144 |  | 0.993 | 720 | 685.6 | 1.050 |
| 60 | 531 |  | 0.973 | 3,586 | 3,343.0 | 1.073 |
| 61 | 392 422.6 |  | 0.928 | 2,104 | 2,498.3 | 0.842 |
| 62 | 472 532.0 |  | 0.887 | 2,066 | 1,975.0 | 1.046 |
| 63 | 362 |  | 1.025 | 1,367 | 1,491.5 | 0.917 |
| 64 | 284 |  | 0.974 | 1,045 | 1,161.0 | 0.900 |
| 65 | 316 |  | 0.823 | 1,306 | 1,306.7 | 0.999 |
| 66 | 346 |  | 1.019 | 1,013 | 1,009.1 | 1.004 |
| 67 | 237 |  | 0.995 | 710 | 670.8 | 1.058 |
| 68 | 180 |  | 0.992 | 454 | 472.5 | 0.961 |
| 69 | 139427 |  | 1.063 | 353 | 357.3 | 0.988 |
| 70 \& Over |  |  | 0.618 | 816 | 1,219.4 | 0.669 |
| TOTAL | 3,972 | 4,458.4 | 0.891 | 16,084 | 16,871.4 | 0.953 |
| 50 \& Under 51 | 30 or more years of service and less than age 65 |  |  |  |  |  |
|  | 47 | 45.6 | 1.031 | 166 | 144.7 | 1.147 |
|  | 66 | 57.6 | 1.146 | 338 | 271.8 | 1.244 |
| 52 | 111 | 95.7 | 1.160 | 607 | 487.8 | 1.244 |
| 53 | 186 | 138.2 | 1.346 | 684 | 501.0 | 1.365 |
| 54 | 167 | 155.6 | 1.073 | 672 | 579.8 | 1.159 |
| 55 | 180 | 181.2 | 0.993 | 705 | 628.3 | 1.122 |
| 56 | 195 | 182.0 | 1.071 | 679 | 607.9 | 1.117 |
| 57 | 170 | 172.1 | 0.988 | 608 | 584.1 | 1.041 |
| 58 | 154 | 153.0 | 1.007 | 609 | 589.7 | 1.033 |
| 59 | 150 | 146.3 | 1.025 | 618 | 591.4 | 1.045 |
| 60 | 140 | 139.0 | 1.007 | 624 | 576.2 | 1.083 |
| 61 | 108 | 112.0 | 0.964 | 504 | 497.9 | 1.012 |
| 62 | 127 | 119.2 | 1.065 | 461 | 444.2 | 1.038 |
| 63 | 72 | 89.1 | 0.808 | 333 | 346.6 | 0.961 |
| 64 | 72 | 81.9 | 0.879 | 272 | 282.1 | 0.964 |
| TOTAL | 1,945 | 1,868.5 | 1.041 | 7,880 | 7,133.5 | 1.105 |

The analysis of the experience reflects that the current assumed rates of retirement slightly overanticipate retirements for members prior to 30 years of service but under-anticipate the rates for those with 30 years or more of service requirements before age 65 , particularly when first achieving 30 years. Fewer retirements than expected create gains to the System, while more than expected create losses, particularly for unreduced retirement at younger ages. We recommend adjustment to the rates to reflect the experience as well as maintain a reasonable degree of margin. The following graphs show a comparison of the present, actual, and proposed rates of service retirements.





The following table shows a comparison of the present and proposed rates of service retirement.

## COMPARATIVE RATES OF RETIREMENT

| AGE | RATES OFSERVICEREIIREMIDNT |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | MALE |  |  |  | FEMALE |  |  |  |
|  | Present |  | Proposed |  | Present |  | Proposed |  |
|  | < $\mathbf{3 0}$ years of service | $\begin{aligned} & >=30 \text { years } \\ & \text { of service } \end{aligned}$ | < 30 years of service | $\begin{aligned} & >=30 \text { years } \\ & \text { of service } \end{aligned}$ | < 30 years of service | $\begin{aligned} & >=30 \text { years } \\ & \text { of service } \end{aligned}$ | $\begin{gathered} <30 \text { years of } \\ \text { service } \end{gathered}$ | $\begin{aligned} & \text { >= } 30 \text { years } \\ & \text { of service } * * \end{aligned}$ |
| 50 | 3.5\% | 60.0\% | 3.0\% | 52.0\% | 3.0\% | 55.0\% | 2.8\% | 50.0\% |
| 51 | 3.5\% | 60.0\% | 3.0\% | 58.0\% | 3.0\% | 60.0\% | 2.8\% | 58.0\% |
| 52 | 3.5\% | 55.0\% | 3.0\% | 54.0\% | 3.0\% | 52.0\% | 2.8\% | 48.0\% |
| 53 | 3.5\% | 45.0\% | 3.0\% | 50.0\% | 3.0\% | 37.0\% | 2.8\% | 35.0\% |
| 54 | 3.5\% | 40.0\% | 3.0\% | 36.0\% | 3.0\% | 37.0\% | 2.8\% | 35.0\% |
| 55 | 5.0\% | 40.0\% | 5.0\% | 37.0\% | 5.5\% | 37.0\% | 5.8\% | 35.0\% |
| 56 | 5.0\% | 38.0\% | 5.0\% | 37.0\% | 5.5\% | 37.0\% | 5.8\% | 35.0\% |
| 57 | 5.0\% | 38.0\% | 5.0\% | 35.0\% | 5.5\% | 38.0\% | 5.8\% | 35.0\% |
| 58 | 5.0\% | 36.0\% | 5.0\% | 33.0\% | 5.5\% | 39.0\% | 5.8\% | 35.0\% |
| 59 | 5.0\% | 35.0\% | 5.0\% | 34.0\% | 5.5\% | 42.0\% | 5.8\% | 40.0\% |
| 60 | 20.0\% | 36.0\% | 20.0\% | 34.0\% | 25.0\% | 43.0\% | 25.0\% | 40.0\% |
| 61 | 18.0\% | 32.0\% | 18.0\% | 30.0\% | 25.0\% | 43.0\% | 25.0\% | 40.0\% |
| 62 | 26.0\% | 36.0\% | 25.0\% | 35.0\% | 25.0\% | 43.0\% | 25.0\% | 43.0\% |
| 63 | 22.0\% | 33.0\% | 22.0\% | 28.0\% | 25.0\% | 43.0\% | 25.0\% | 43.0\% |
| 64 | 22.0\% | 32.0\% | 22.0\% | 28.0\% | 25.0\% | 43.0\% | 24.0\% | 43.0\% |
| 65 | 30.0\% | 30.0\% | 27.0\% | 27.0\% | 31.0\% | 31.0\% | 32.0\% | 32.0\% |
| 66 | 32.0\% | 32.0\% | 32.0\% | 32.0\% | 33.0\% | 33.0\% | 32.0\% | 32.0\% |
| 67 | 30.0\% | 30.0\% | 30.0\% | 30.0\% | 30.0\% | 30.0\% | 32.0\% | 32.0\% |
| 68 | 30.0\% | 30.0\% | 30.0\% | 30.0\% | 30.0\% | 30.0\% | 30.0\% | 30.0\% |
| 69 | 28.0\% | 28.0\% | 30.0\% | 30.0\% | 30.0\% | 30.0\% | 30.0\% | 30.0\% |
| 70 | 30.0\% | 30.0\% | 30.0\% | 30.0\% | 30.0\% | 30.0\% | 30.0\% | 30.0\% |
| 71 | 25.0\% | 25.0\% | 30.0\% | 30.0\% | 30.0\% | 30.0\% | 30.0\% | 30.0\% |
| 72 | 25.0\% | 25.0\% | 30.0\% | 30.0\% | 30.0\% | 30.0\% | 30.0\% | 30.0\% |
| 73 | 25.0\% | 25.0\% | 30.0\% | 30.0\% | 30.0\% | 30.0\% | 30.0\% | 30.0\% |
| 74 | 25.0\% | 25.0\% | 30.0\% | 30.0\% | 30.0\% | 30.0\% | 30.0\% | 30.0\% |
| 75 | 100.0\% | 100.0\% | 100.0\% | 100.0\% | 100.0\% | 100.0\% | 100.0\% | 100.0\% |

[^0]
## COMPARISON OF ACTUAL AND EXPECTED RETIREMENTS

 BASED ON PROPOSED RATES OF RETIREMENT| $\begin{aligned} & \text { CENTRAL } \\ & \text { AGE } \\ & \text { OF GROUP } \end{aligned}$ | NUMIBER OF SERVICE RETIREMIDNTS |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | MALE |  |  | FEMALE |  |  |
|  | Actual | Expected | Ratio of Actual to Expected | Actual | Expected | Ratio of Actual to Expected |
| 49 \& Under <br> 52 | Less than 30 years of service or all ages 65 and over |  |  |  |  |  |
|  | 18 | 33.8 | 0.533 | 98 | 133.1 | 0.736 |
|  | 124 | 140.5 | 0.883 | 446 | 471.9 | 0.945 |
| 57 | 144 | 145.0 | 0.993 | 720 | 716.8 | 1.004 |
| 60 | 531 | 545.6 | 0.973 | 3,586 | 3,343.0 | 1.073 |
| 61 | 392 | 422.6 | 0.928 | 2,104 | 2,498.3 | 0.842 |
| 62 | 472 | 511.5 | 0.923 | 2,066 | 1,975.0 | 1.046 |
| 63 | 362 | 353.3 | 1.025 | 1,367 | 1,491.5 | 0.917 |
| 64 | 284 | 291.7 | 0.974 | 1,045 | 1,114.6 | 0.938 |
| 65 | 316 | 345.6 | 0.914 | 1,306 | 1,348.8 | 0.968 |
| 66 | 346 | 339.5 | 1.019 | 1,013 | 978.6 | 1.035 |
| 67 | 237 | 238.2 | 0.995 | 710 | 715.5 | 0.992 |
| 68 | 180 | 181.5 | 0.992 | 454 | 472.5 | 0.961 |
| 69 | 139 | 140.1 | 0.992 | 353 | 357.3 | 0.988 |
| 70 \& Over | 427 | 729.4 | 0.585 | 816 | 1,219.4 | 0.669 |
| TOTAL | 3,972 | 4,418.3 | 0.899 | 16,084 | 16,836.3 | 0.955 |
| $\begin{gathered} 50 \& \text { Under } \\ 51 \end{gathered}$ | 30 or more years of servicce and less than age 65 |  |  |  |  |  |
|  | 47 | 46.9 | 1.002 | 166 | 156.6 | 1.060 |
|  | 66 | 62.6 | 1.054 | 338 | 307.9 | 1.098 |
| 52 | 111 | 104.5 | 1.062 | 607 | 542.2 | 1.120 |
| 53 | 186 | 171.5 | 1.085 | 684 | 585.1 | 1.169 |
| 54 | 167 | 158.5 | 1.054 | 672 | 649.9 | 1.034 |
| 55 | 180 | 183.2 | 0.983 | 705 | 682.7 | 1.033 |
| 56 | 195 | 192.2 | 1.015 | 679 | 648.4 | 1.047 |
| 57 | 170 | 169.5 | 1.003 | 608 | 596.6 | 1.019 |
| 58 | 154 | 152.2 | 1.012 | 609 | 587.7 | 1.036 |
| 59 | 150 | 151.3 | 0.991 | 618 | 620.5 | 0.996 |
| 60 | 140 | 139.2 | 1.006 | 624 | 598.0 | 1.043 |
| 61 | 108 | 111.1 | 0.972 | 504 | 503.9 | 1.000 |
| 62 | 127 | 120.4 | 1.055 | 461 | 444.2 | 1.038 |
| 63 | 72 | 80.0 | 0.900 | 333 | 346.6 | 0.961 |
| 64 | 72 | 75.4 | 0.955 | 272 | 282.1 | 0.964 |
| TOTAL | 1,945 | 1,918.5 | 1.014 | 7,880 | 7,552.4 | 1.043 |

## RATES OF PRE-RETIREMENT MORTALITY

COMPARISON OF ACTUAL AND EXPECTED PRE-RETIREMENT MORTALITY

| $\begin{gathered} \text { CENTRAL } \\ \text { AGE } \\ \text { OF GROUP } \end{gathered}$ | NUMIBER OF DEATHS |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | MALE |  |  | FEMALE |  |  |
|  | Actual | Expected | Ratio of Actual to Expected | Actual | Expected | Ratio of Actual to Expected |
| 27 \& Under | 2 | 4.4 | 0.455 | 1 | 8.8 | 0.114 |
| 30 | 4 | 10.8 | 0.370 | 9 | 21.2 | 0.425 |
| 35 | 9 | 22.8 | 0.395 | 14 | 44.8 | 0.313 |
| 40 | 12 | 34.6 | 0.347 | 34 | 77.0 | 0.442 |
| 45 | 24 | 52.2 | 0.460 | 57 | 142.5 | 0.400 |
| 50 | 35 | 66.3 | 0.528 | 66 | 198.1 | 0.333 |
| 53 \& Over | 91 | 265.2 | 0.343 | 177 | 678.7 | 0.261 |
| TOTAL | 177 | 456.3 | 0.388 | 358 | 1,171.1 | 0.306 |

The experience indicates that the pre-retirement mortality rates were significantly lower than anticipated. However, death in active service accounts for a very small part of the liability of the System and the small number of deaths don't provide creditable data for analysis. Therefore, we are recommending the same tables and adjustments that we are recommending for post-retirement. We recommend that the rates of mortality in active service for both males and females be changed to the Pub-2010 Teachers Headcount Weighted Below Median Employee mortality table with ages set forward one year and adjusted $106 \%$. Future improvement in mortality rates is assumed using the MP-2019 projection scale generationally. The rates of improvement have been reduced by $20 \%$ for all years prior to the ultimate rate. The following table shows a comparison between the present death rates and the proposed rates. The proposed rates shown below are based on a projection to 2015. Actual mortality rates would be projected generationally. Generational mortality projection is discussed in the next section.

COMPARATIVE RATES OF PRE-RETIREMENT MORTALITY

| AGE | RATES OF MORTALITY |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | MALE |  |  |  |
|  | Present | Proposed* | Present | Proposed* |
|  |  |  |  |  |
| 20 | $0.0320 \%$ | $0.0375 \%$ | $0.0177 \%$ | $0.0139 \%$ |
| 25 | $0.0349 \%$ | $0.0336 \%$ | $0.0192 \%$ | $0.0148 \%$ |
| 30 | $0.0412 \%$ | $0.0437 \%$ | $0.0245 \%$ | $0.0235 \%$ |
| 35 | $0.0717 \%$ | $0.0549 \%$ | $0.0441 \%$ | $0.0345 \%$ |
| 40 | $0.1001 \%$ | $0.0714 \%$ | $0.0655 \%$ | $0.0493 \%$ |
| 45 | $0.1399 \%$ | $0.1087 \%$ | $0.1043 \%$ | $0.0728 \%$ |
| 50 | $0.1983 \%$ | $0.1799 \%$ | $0.1555 \%$ | $0.1107 \%$ |
| 55 | $0.2810 \%$ | $0.2828 \%$ | $0.2228 \%$ | $0.1687 \%$ |
| 60 | $0.4092 \%$ | $0.4441 \%$ | $0.3058 \%$ | $0.2554 \%$ |
| 64 | $0.5330 \%$ | $0.6475 \%$ | $0.4015 \%$ | $0.3665 \%$ |

*Rates as of 2015

## RATES OF POST-RETIREMENT MORTALITY

The current basis for rate of post-retirement mortality for service retirees and beneficiaries the RP2000 White Collar Mortality Table with future mortality improvement projected to 2025 with the Society of Actuaries' projection scale BB set forward one year for males. The current basis for rate of post-retirement mortality for disability retirees is the RP-2000 Disabled Mortality Table with future mortality improvement projected to 2025 with Society of Actuaries' projection scale BB set forward two years for males and four years for females.

## COMPARISON OF ACTUAL AND EXPECTED CASES OF POST-RETIREMENT DEATHS

| $\begin{gathered} \text { CENTRAL } \\ \text { AGE } \\ \text { OF GROUP } \end{gathered}$ | NUMIBER OF DEATHS AMONG SERVICE RETIREMIDNTS AND BENDFICIARIES |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | MALE |  |  | FEMALE |  |  |
|  | Actual | Expected | Ratio of Actual to Expected | Actual | Expected | Ratio of Actual to Expected |
| 47 \& Under | 12 | 2.8 | 4.286 | 7 | 1.9 | 3.684 |
| 50 | 5 | 3.1 | 1.613 | 7 | 4.2 | 1.667 |
| 55 | 36 | 18.1 | 1.989 | 56 | 42.2 | 1.327 |
| 60 | 106 | 78.2 | 1.355 | 239 | 225.8 | 1.058 |
| 65 | 277 | 270.0 | 1.026 | 672 | 745.0 | 0.902 |
| 70 | 436 | 425.2 | 1.025 | 881 | 1,029.8 | 0.856 |
| 75 | 563 | 516.9 | 1.089 | 945 | 1,053.6 | 0.897 |
| 80 | 663 | 599.9 | 1.105 | 1,193 | 1,096.0 | 1.089 |
| 85 | 652 | 628.0 | 1.038 | 1,390 | 1,189.0 | 1.169 |
| 90 | 449 | 443.3 | 1.013 | 1,308 | 964.7 | 1.356 |
| 93 \& Over | 236 | 213.1 | 1.107 | 1,040 | 814.1 | 1.277 |
| TOTAL | 3,435 | 3,198.6 | 1.074 | 7,738 | 7,166.3 | 1.080 |


| $\begin{gathered} \text { CENTRAL } \\ \text { AGE } \\ \text { OF GROUP } \end{gathered}$ | NUMIBER OF DEATHS AMONG DISABILITY RETIREMIDNTS |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | MALE |  |  | FEMALE |  |  |
|  | Actual | Expected | Ratio of Actual to Expected | Actual | Expected | Ratio of Actual to Expected |
| 47 \& Under | 8 | 3.4 | 2.353 | 30 | 7.0 | 4.286 |
| 50 | 11 | 9.8 | 1.122 | 15 | 16.7 | 0.898 |
| 55 | 28 | 19.7 | 1.421 | 64 | 45.5 | 1.407 |
| 60 | 34 | 33.2 | 1.024 | 107 | 83.2 | 1.286 |
| 65 | 28 | 28.6 | 0.979 | 85 | 98.5 | 0.863 |
| 70 | 29 | 24.3 | 1.193 | 75 | 86.4 | 0.868 |
| 75 | 20 | 20.2 | 0.990 | 61 | 60.4 | 1.010 |
| 80 | 8 | 13.0 | 0.615 | 33 | 36.5 | 0.904 |
| 85 | 5 | 7.7 | 0.649 | 32 | 34.4 | 0.930 |
| 90 | 5 | 3.6 | 1.389 | 27 | 24.9 | 1.084 |
| 93 \& Over | 1 | 0.5 | 2.000 | 15 | 12.7 | 1.181 |
| TOTAL | 177 | 164.0 | 1.079 | 544 | 506.2 | 1.075 |

There are two widely used approaches for reflecting future improvements in mortality:
(1) Static table with "margin"
(2) Generational mortality.

The first approach to reflecting mortality improvements is through the use of a static mortality table with "margin." Under this approach, the mortality assumption will include a margin (lower mortality rates than experienced) to account for a reasonable degree of future improvement. While there is no formal guidance for the amount of margin required (how far above $100 \%$ is appropriate for the $\mathrm{A} / \mathrm{E}$ ratio), we typically prefer to have a margin of around $10 \%$ at the core retirement ages. The goal is still for the general shape of the curve to be a reasonable fit to the observed experience. Depending on the magnitude and duration of actual mortality improvements in the future, the margin may decrease and eventually become insufficient. If and when that occurs, the assumption would need to be updated.

The more modern approach, referred to as generational mortality, directly anticipates future improvements in mortality by using a different set of mortality rates for each year of birth, with the rates for later years of birth assuming lower mortality than the rates for earlier years of birth. The varying mortality rates by year of birth create a series of tables that contain "built-in" mortality improvements, e.g., a member who turns age 65 in 2035 has a longer life expectancy than a member who turns age 65 in 2020. When using generational mortality, the $\mathrm{A} / \mathrm{E}$ ratios for the observed experience are set near $100 \%$ as future mortality improvements will be included through the generational projection of mortality improvement eliminating the need to include a margin in the rates.

The mortality assumption used during the study period has maintained a reasonable margin appropriate for the static projection of mortality improvement. With this experience study, we recommend the adoption of a generational projection of mortality improvement. This method of projecting improvement utilizes an age specific rate of improvement in mortality rates for each future year which are produced from analysis published by the Society of Actuaries. The selected improvement scale, the most recently published MP-2019 improvement scale, is applied to a base mortality table which should reasonably reflect the current mortality experience of the studied population. For service retirees and beneficiaries, we recommend the base mortality table use of the Pub-2010 Teachers Headcount Weighted Below Median Healthy Retiree mortality table with ages set forward one year and adjusted $106 \%$ as the base mortality table. Future improvement in mortality rates is reflected by applying the MP-2019 projection scale generationally. The rates of improvement have been reduced by $20 \%$ for all years prior to the ultimate rate. This reduction in the projected improvement rates is based on our review of the actual rates of improvement measured in the mortality experience of retirees and beneficiaries from the three prior experience studies. Based on our analysis, the rates of improvement realized have been over $20 \%$ less than those expected under the MP-2019 improvement scale. We recommend reducing the MP-2019 improvement rates by $20 \%$ for all years prior to 2035, the year that ultimate rates are in effect, and $100 \%$ of the ultimate rate of improvement thereafter.

Disability retirement accounts for a very small part of the liability of the System and the small number of disabilities don't provide creditable data for analysis. Therefore, we are recommending
the same tables and adjustments that we are recommending for service retirement. We recommend that for disability retirements, the Pub-2010 Teachers Mortality Table for Disabled Retirees with ages set forward one year and adjusted $106 \%$. Future improvement in mortality rates is assumed using the MP-2019 projection scale generationally. The rates of improvement have been reduced by $20 \%$ for all years prior to the ultimate rate. The following graphs show a comparison of the present, actual and proposed rates of post-retirement mortality. The proposed rates shown in the graphs are based on the tables described above, projected to 2015, which is the mid-point of the experience study period and were the rates used to set the rates of healthy mortality going forward. Note that actual and proposed rates track fairly well.





The following table shows a comparison of the present and proposed rates of post-retirement mortality. The proposed rates shown below are based on a projection to 2015. Actual mortality rates will be projected generationally to the year of the measurement.

## COMPARATIVE RATES OF POST-RETIREMENT MORTALITY

| AGE | SERVICERETIREMIENTS AND BENDFICIARIES |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | MALE |  | FEMALE |  |
|  | Present | Proposed** | Present | Proposed\% |
| 35 | 0.0602\% | 0.0549\% | 0.0432\% | 0.0345\% |
| 40 | 0.0889\% | 0.0714\% | 0.0598\% | 0.0493\% |
| 45 | 0.1352\% | 0.1087\% | 0.0942\% | 0.0728\% |
| 50 | 0.2136\% | 0.1799\% | 0.1474\% | 0.1107\% |
| 55 | 0.3478\% | 0.5241\% | 0.2281\% | 0.3901\% |
| 60 | 0.5197\% | 0.6440\% | 0.3638\% | 0.4136\% |
| 65 | 0.9071\% | 0.8433\% | 0.6397\% | 0.5260\% |
| 70 | 1.4666\% | 1.4580\% | 1.1229\% | 0.9329\% |
| 75 | 2.5894\% | 2.7028\% | 1.9017\% | 1.7905\% |
| 80 | 4.5768\% | 4.9635\% | 3.1857\% | 3.4310\% |
| 85 | 8.0034\% | 9.0522\% | 5.4864\% | 6.5905\% |
| 90 | 15.1656\% | 16.0712\% | 9.5675\% | 12.3050\% |

*Rates as of 2015

| AGE | DISABIIITY RETIREMIDNTS |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | MALE |  |  |  |
|  | Present | Proposed* | Present | Proposed* |
|  |  |  |  |  |
| 35 | $2.0938 \%$ | $0.6444 \%$ | $0.6911 \%$ | $0.5093 \%$ |
| 40 | $2.0938 \%$ | $0.8444 \%$ | $0.6911 \%$ | $0.7386 \%$ |
| 45 | $2.3306 \%$ | $1.2146 \%$ | $0.9865 \%$ | $1.1004 \%$ |
| 50 | $2.9279 \%$ | $1.8432 \%$ | $1.4019 \%$ | $1.6181 \%$ |
| 55 | $3.4400 \%$ | $2.4790 \%$ | $1.6567 \%$ | $1.9679 \%$ |
| 60 | $3.5881 \%$ | $3.0569 \%$ | $1.9670 \%$ | $2.2548 \%$ |
| 65 | $3.8275 \%$ | $3.7177 \%$ | $2.6129 \%$ | $2.6170 \%$ |
| 70 | $4.7566 \%$ | $4.6328 \%$ | $3.6157 \%$ | $3.3740 \%$ |
| 75 | $6.3153 \%$ | $6.1798 \%$ | $5.0131 \%$ | $4.7842 \%$ |
| 80 | $8.3527 \%$ | $8.8648 \%$ | $6.9358 \%$ | $7.2311 \%$ |
| 85 | $10.9122 \%$ | $13.0223 \%$ | $9.6851 \%$ | $11.2015 \%$ |
| 90 | $17.2787 \%$ | $18.8001 \%$ | $15.3358 \%$ | $16.0832 \%$ |

[^1]
## COMPARISON OF ACTUAL AND EXPECTED CASES OF POST-RETIREMENT DEATHS BASED ON PROPOSED RATES OF MORTALITY

| $\begin{gathered} \text { CENTRAL } \\ \text { AGE } \\ \text { OF GROUP } \end{gathered}$ | NUMIBER OF DEATHS AMONG SERVICE RETIRIEMIDNTS AND BENDFICIARIES |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | MALE |  |  | FEMALE |  |  |
|  | Actual | Expected | Ratio of Actual to Expected | Actual | Expected | Ratio of Actual to Expected |
| 47 \& Under | 12 | 2.4 | 5.000 | 7 | 1.5 | 4.667 |
| 50 | 5 | 2.7 | 1.852 | 7 | 3.1 | 2.258 |
| 55 | 36 | 26.0 | 1.385 | 56 | 63.5 | 0.882 |
| 60 | 106 | 91.8 | 1.155 | 239 | 244.4 | 0.978 |
| 65 | 277 | 257.7 | 1.075 | 672 | 617.4 | 1.088 |
| 70 | 436 | 423.8 | 1.029 | 881 | 862.6 | 1.021 |
| 75 | 563 | 539.8 | 1.043 | 945 | 992.4 | 0.952 |
| 80 | 663 | 651.0 | 1.018 | 1,193 | 1,181.5 | 1.010 |
| 85 | 652 | 699.7 | 0.932 | 1,390 | 1,427.0 | 0.974 |
| 90 | 449 | 472.0 | 0.951 | 1,308 | 1,239.0 | 1.056 |
| 93 \& Over | 236 | 225.6 | 1.046 | 1,040 | 1,114.1 | 0.933 |
| TOTAL | 3,435 | 3,392.5 | 1.013 | 7,738 | 7,746.5 | 0.999 |


| $\begin{aligned} & \text { CENTRAL } \\ & \text { AGE } \\ & \text { OF GROUP } \end{aligned}$ | NUMBER OF DEATHS AMONG DISABILITY RETIREMIENTS |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | MALE |  |  | FIMMALE |  |  |
|  | Actual | Expected | Ratio of Actual to Expected | Actual | Expected | Ratio of Actual to Expected |
| 47 \& Under | 8 | 1.7 | 4.706 | 30 | 7.7 | 3.896 |
| 50 | 11 | 6.2 | 1.774 | 15 | 19.3 | 0.777 |
| 55 | 28 | 14.4 | 1.944 | 64 | 54.2 | 1.181 |
| 60 | 34 | 28.3 | 1.201 | 107 | 95.0 | 1.126 |
| 65 | 28 | 27.6 | 1.014 | 85 | 98.9 | 0.859 |
| 70 | 29 | 23.8 | 1.218 | 75 | 81.0 | 0.926 |
| 75 | 20 | 19.8 | 1.010 | 61 | 57.7 | 1.057 |
| 80 | 8 | 13.7 | 0.584 | 33 | 38.0 | 0.868 |
| 85 | 5 | 9.2 | 0.543 | 32 | 39.0 | 0.821 |
| 90 | 5 | 4.0 | 1.250 | 27 | 26.3 | 1.027 |
| 93 \& Over | 1 | 0.5 | 2.000 | 15 | 13.9 | 1.079 |
| TOTAL | 177 | 149.2 | 1.186 | 544 | 531.0 | 1.024 |

## RATES OF SALARY INCREASE

## COMPARISON OF ACTUAL AND EXPECTED RATES OF SALARY INCREASE OF ACTIVE MEMBERS

| SERVICE | SALARIES AT END OF YEAR (\$1,000's) |  |  |
| :---: | :---: | :---: | :---: |
|  | Actual | Expected | Ratio of Actual to Expected |
| 0 | 311,756 | 258,929 | 1.204 |
| 1 | 3,016,994 | 2,863,932 | 1.053 |
| 2 | 2,532,956 | 2,511,197 | 1.009 |
| 3 | 2,152,239 | 2,136,553 | 1.007 |
| 4 | 1,834,694 | 1,820,922 | 1.008 |
| 5 | 1,783,059 | 1,777,909 | 1.003 |
| 6 | 1,918,042 | 1,910,237 | 1.004 |
| 7 | 2,122,321 | 2,105,504 | 1.008 |
| 8 | 2,318,565 | 2,302,946 | 1.007 |
| 9 | 2,455,039 | 2,432,705 | 1.009 |
| 10 | 2,356,426 | 2,342,362 | 1.006 |
| 11 | 2,252,797 | 2,232,660 | 1.009 |
| 12 | 2,135,689 | 2,130,926 | 1.002 |
| 13 | 2,046,370 | 2,034,281 | 1.006 |
| 14 | 1,978,624 | 1,971,023 | 1.004 |
| 15 | 1,955,841 | 1,942,062 | 1.007 |
| 16 | 1,855,912 | 1,849,616 | 1.003 |
| 17 | 1,726,555 | 1,712,781 | 1.008 |
| 18 | 1,611,946 | 1,607,890 | 1.003 |
| 19 | 1,516,822 | 1,506,302 | 1.007 |
| 20 \& Over | 10,473,630 | 10,514,000 | 0.996 |
| Total | 50,356,277 | 49,964,737 | 1.008 |

The current assumed rates of salary increase were somewhat greater than the actual rates of increase averaged over the study period in most service categories. However, we believe that salary increases during the study period were not necessarily indicative of the expected long-term future rate of salary increase. Therefore, we recommend no change to the current salary increase rates at this time.

## Section V <br> Other Assumptions and Methods and Administrative Procedures

ADMINISTRATIVE EXPENSES: This assumption is currently $0.25 \%$ of payroll (included in normal contribution). The actual administrative expenses over the experience study period have been approximately $0.20 \%$ of payroll. We recommend a change in this assumption to $0.20 \%$ of payroll.

ASSETS: Currently, the actuarial value of assets recognizes a portion of the difference between the market value of assets and the expected actuarial value of assets, based on the assumed valuation rate of return. The amount recognized each year is $20 \%$ of the difference between market value and expected actuarial value. We recommend maintaining the current smoothing method.

COST OF LIVING: Currently, we assume cost of living increases of $1.5 \%$ semi-annually. We recommend maintaining this assumption.

OPTION FACTORS: The option factors currently used by the Retirement System are based on the mortality tables and investment rate of return (discount rate) used in the valuation. We recommend that the factors be revised to be based on the mortality table recommended for the valuation.

PERCENT MARRIED: This assumption is used to determine who will receive death in active service benefits. The beneficiaries of unmarried members are assumed to receive a refund of member contributions. We recommend keeping this assumption for death in active service benefits as $100 \%$ married for both males and females.

UNUSED SICK LEAVE: Currently, we assume a $1.25 \%$ load on liabilities for members who retire on early retirement, a $1.25 \%$ load for members who retire with unreduced retirement before 30 years of service and a $1.75 \%$ load for members who retire with 30 or more years of service. Based on data we received from the Retirement System on members who converted unused leave at retirement over the past five years, we recommend changing the loads on liabilities to $1.50 \%$ for members who retire on early retirement and for members who retire with unreduced retirement before 30 years of service and a $2.00 \%$ load for members who retire with 30 or more years of service.

VALUATION COST METHOD: Currently, the valuation uses the entry age actuarial cost method. This is the most widely used cost method of large public sector plans and has demonstrated the highest degree of stability as compared to alternative methods. We recommend no change to this assumption.

VESTED TERMINATION BENEFIT ELECTION: Currently, we assume that $60 \%$ of vested members under age 50 and $80 \%$ of members age 50 and over who terminate with 10 or more years of service before retirement eligibility will choose to receive a benefit payable at age 60 . Other members are assumed to receive a refund of contribution. Based on the latest experience, we recommend changing the percentage who will elect to receive a benefit to $70 \%$ for those who terminate before age 50 and leaving the percentage who will elect to receive a benefit as $80 \%$ for members who terminate at age 50 and over.

## APPENDIX A

Historical June CPI (U) Index

| Fiscal Year <br> Ending 6/30 | CPI (U) | Fiscal Year <br> Ending 6/30 | CPI (U) |
| :---: | :---: | :---: | :--- |
| 1964 | 31.0 | 1992 | 140.2 |
| 1965 | 31.6 | 1993 | 144.4 |
| 1966 | 32.4 | 1994 | 148.0 |
| 1967 | 33.3 | 1995 | 152.5 |
| 1968 | 34.7 | 1996 | 156.7 |
| 1969 | 36.6 | 1997 | 160.3 |
| 1970 | 38.8 | 1998 | 163.0 |
| 1971 | 40.6 | 1999 | 166.2 |
| 1972 | 41.7 | 2000 | 172.4 |
| 1973 | 44.2 | 2001 | 178.0 |
| 1974 | 49.0 | 2002 | 179.9 |
| 1975 | 53.6 | 2003 | 183.7 |
| 1976 | 56.8 | 2004 | 189.7 |
| 1977 | 60.7 | 2005 | 194.5 |
| 1978 | 65.2 | 2006 | 202.9 |
| 1979 | 72.3 | 2007 | 208.352 |
| 1980 | 82.7 | 2008 | 218.815 |
| 1981 | 90.6 | 2009 | 215.693 |
| 1982 | 97.0 | 2010 | 217.965 |
| 1983 | 99.5 | 2011 | 225.722 |
| 1984 | 103.7 | 2012 | 229.478 |
| 1985 | 107.6 | 2013 | 233.504 |
| 1986 | 109.5 | 2014 | 238.343 |
| 1987 | 113.5 | 2015 | 241.638 |
| 1988 | 118.0 | 2016 | 244.955 |
| 1989 | 124.1 | 2017 |  |
| 1990 | 129.9 | 2018 |  |
| 1991 | 136.0 |  | 289 |
|  |  |  |  |

## APPENDIX B

## Capital Market Assumptions and Asset Allocation

## Real Rates of Return and Standard Deviations by Asset Class

| Asset Class | Expected Real Rate of Return* | Standard Deviation |
| :--- | :---: | :---: |
| Fixed Income | $-0.1 \%$ | $4.7 \%$ |
| Domestic Large Cap Stocks | $8.9 \%$ | $19.8 \%$ |
| Domestic Small Cap Stocks | $13.2 \%$ | $31.6 \%$ |
| Int'l Developed Mkt Stocks | $8.9 \%$ | $21.8 \%$ |
| Int'l Emerging Mkt Stocks | $5.1 \%$ | $31.7 \%$ |

*Net of inflation

## Asset Class Correlation Coefficients

| Asset Class | Fixed <br> Income | US <br> Large <br> Stocks | US <br> Small <br> Stocks | Int'l Dev <br> Mkt <br> Stocks | Int'l EM <br> Mkt <br> Stocks |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Fixed Income | 1.00 |  |  |  |  |
| Domestic Large Cap Stocks | 0.00 | 1.00 |  |  |  |
| Domestic Small Cap Stocks | -0.10 | 0.79 | 1.00 |  |  |
| Int'l Developed Mkt Stocks | -0.11 | 0.67 | 0.51 | 1.00 |  |
| Int'l Emerging Mkt Stocks | -0.11 | 0.67 | 0.51 | 0.71 | 1.00 |

## Asset Allocation Targets

| Asset Class | Asset Allocation |
| :--- | :---: |
| Fixed Income | $30.0 \%$ |
| Domestic Large Cap Stocks | $51.0 \%$ |
| Domestic Small Cap Stocks | $1.5 \%$ |
| Int'l Developed Mkt Stocks | $12.4 \%$ |
| Int'l Emerging Mkt Stocks | $5.1 \%$ |

## APPENDIX C

Social Security Administration Calendar Year Wage Index

| Calendar <br> Year | Wage Index | Annual <br> Increase | Calendar <br> Year | Wage Index | Annual <br> Increase |
| :---: | ---: | :---: | :---: | :---: | :---: |
| 1963 | $\$ 4,396.64$ |  | 1991 | $\$ 21,811.60$ | $3.73 \%$ |
| 1964 | $4,576.32$ | $4.09 \%$ | 1992 | $22,935.42$ | 5.15 |
| 1965 | $4,658.72$ | 1.80 | 1993 | $23,132.67$ | 0.86 |
| 1966 | $4,938.36$ | 6.00 | 1994 | $23,753.53$ | 2.68 |
| 1967 | $5,213.44$ | 5.57 | 1995 | $24,705.66$ | 4.01 |
| 1968 | $5,571.76$ | 6.87 | 1996 | $25,913.90$ | 4.89 |
| 1969 | $5,893.76$ | 5.78 | 1997 | $27,426.00$ | 5.84 |
| 1970 | $6,186.24$ | 4.96 | 1998 | $28,861.44$ | 5.23 |
| 1971 | $6,497.08$ | 5.02 | 1999 | $30,469.84$ | 5.57 |
| 1972 | $7,133.80$ | 9.80 | 2000 | $32,154.82$ | 5.53 |
| 1973 | $7,580.16$ | 6.26 | 2001 | $32,921.92$ | 2.39 |
| 1974 | $8,030.76$ | 5.94 | 2002 | $33,252.09$ | 1.00 |
| 1975 | $8,630.92$ | 7.47 | 2003 | $34,064.95$ | 2.44 |
| 1976 | $9,226.48$ | 6.90 | 2004 | $35,648.55$ | 4.65 |
| 1977 | $9,779.44$ | 5.99 | 2005 | $36,952.94$ | 3.66 |
| 1978 | $10,556.03$ | 7.94 | 2006 | $38,651.41$ | 4.60 |
| 1979 | $11,479.46$ | 8.75 | 2007 | $40,405.48$ | 4.54 |
| 1980 | $12,513.46$ | 9.01 | 2008 | $41,334.97$ | 2.30 |
| 1981 | $13,773.10$ | 10.07 | 2009 | $40,711.61$ | $(1.51)$ |
| 1982 | $14,531.34$ | 5.51 | 2010 | $41,673.83$ | 2.36 |
| 1983 | $15,239.24$ | 4.87 | 2011 | $42,979.61$ | 3.13 |
| 1984 | $16,135.07$ | 5.88 | 2012 | $44,321.67$ | 3.12 |
| 1985 | $16,822.51$ | 4.26 | 2013 | $44,888.16$ | 1.28 |
| 1986 | $17,321.82$ | 2.97 | 2014 | $46,481.52$ | 3.55 |
| 1987 | $18,426.51$ | 6.38 | 2015 | $48,098.63$ | 3.48 |
| 1988 | $19,334.04$ | 4.93 | 2016 | $48,642.15$ | 1.13 |
| 1989 | $20,099.55$ | 3.96 | 2017 | $50,321.89$ | 3.45 |
| 1990 | $21,027.98$ | 4.62 |  |  |  |
|  |  |  |  |  |  |

## APPENDIX D

TABLE 1
RATES OF SEPARATION FROM ACTIVE SERVICE - MALES

| AGE | Rates of Withdrawal Service |  |  | Death* | Disability | Rates of Retirement |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0-4 | 5-9 | 10+ |  |  | <30 years of service | $\begin{gathered} \text { >= } 30 \text { years } \\ \text { of service } * * \end{gathered}$ |
| 19 | 0.27000 | 0.00000 | 0.00000 | 0.000391 | 0.000000 |  |  |
| 20 | 0.27000 | 0.00000 | 0.00000 | 0.000375 | 0.000000 |  |  |
| 21 | 0.27000 | 0.00000 | 0.00000 | 0.000358 | 0.000000 |  |  |
| 22 | 0.27000 | 0.00000 | 0.00000 | 0.000331 | 0.000000 |  |  |
| 23 | 0.22000 | 0.13000 | 0.00000 | 0.000315 | 0.000000 |  |  |
| 24 | 0.20000 | 0.13000 | 0.00000 | 0.000320 | 0.000000 |  |  |
| 25 | 0.17000 | 0.13000 | 0.00000 | 0.000336 | 0.000000 |  |  |
| 26 | 0.16000 | 0.13000 | 0.00000 | 0.000352 | 0.000000 |  |  |
| 27 | 0.15000 | 0.13000 | 0.00000 | 0.000379 | 0.000000 |  |  |
| 28 | 0.14000 | 0.10000 | 0.08000 | 0.000395 | 0.000000 |  |  |
| 29 | 0.14000 | 0.08000 | 0.07000 | 0.000422 | 0.000000 |  |  |
| 30 | 0.14000 | 0.06500 | 0.06000 | 0.000437 | 0.000000 |  |  |
| 31 | 0.14000 | 0.06500 | 0.06000 | 0.000463 | 0.000000 |  |  |
| 32 | 0.14000 | 0.06500 | 0.06000 | 0.000487 | 0.000000 |  |  |
| 33 | 0.14000 | 0.06250 | 0.04000 | 0.000509 | 0.000125 |  |  |
| 34 | 0.14000 | 0.06250 | 0.03500 | 0.000530 | 0.000145 |  |  |
| 35 | 0.14000 | 0.06250 | 0.03500 | 0.000549 | 0.000165 |  |  |
| 36 | 0.14000 | 0.06250 | 0.03500 | 0.000577 | 0.000185 |  |  |
| 37 | 0.14000 | 0.06250 | 0.03500 | 0.000603 | 0.000205 |  |  |
| 38 | 0.13000 | 0.06250 | 0.03250 | 0.000638 | 0.000225 |  |  |
| 39 | 0.13000 | 0.06250 | 0.03250 | 0.000671 | 0.000250 |  |  |
| 40 | 0.13000 | 0.06250 | 0.02750 | 0.000714 | 0.000275 | 0.03000 |  |
| 41 | 0.13000 | 0.06250 | 0.02750 | 0.000766 | 0.000300 | 0.03000 |  |
| 42 | 0.13000 | 0.06250 | 0.02750 | 0.000827 | 0.000325 | 0.03000 |  |
| 43 | 0.13000 | 0.06000 | 0.02750 | 0.000899 | 0.000560 | 0.03000 |  |
| 44 | 0.13000 | 0.06000 | 0.02500 | 0.000982 | 0.000640 | 0.03000 |  |
| 45 | 0.13000 | 0.06000 | 0.02500 | 0.001087 | 0.000720 | 0.03000 | 0.65000 |
| 46 | 0.13000 | 0.06000 | 0.02500 | 0.001204 | 0.000800 | 0.03000 | 0.65000 |
| 47 | 0.13000 | 0.06000 | 0.02500 | 0.001324 | 0.000880 | 0.03000 | 0.65000 |
| 48 | 0.11250 | 0.05750 | 0.02750 | 0.001468 | 0.000960 | 0.03000 | 0.65000 |
| 49 | 0.11250 | 0.05750 | 0.02750 | 0.001626 | 0.001040 | 0.03000 | 0.65000 |
| 50 | 0.11250 | 0.05750 | 0.02750 | 0.001799 | 0.001360 | 0.03000 | 0.52000 |
| 51 | 0.11250 | 0.05500 | 0.02750 | 0.001977 | 0.001760 | 0.03000 | 0.58000 |
| 52 | 0.11250 | 0.05500 | 0.03000 | 0.002169 | 0.002160 | 0.03000 | 0.54000 |
| 53 | 0.11500 | 0.05500 | 0.03250 | 0.002375 | 0.002240 | 0.03000 | 0.50000 |
| 54 | 0.11500 | 0.05500 | 0.03250 | 0.002595 | 0.002320 | 0.03000 | 0.36000 |
| 55 | 0.11750 | 0.05500 | 0.03250 | 0.002828 | 0.002400 | 0.05000 | 0.37000 |
| 56 | 0.11750 | 0.05750 | 0.03500 | 0.003083 | 0.002560 | 0.05000 | 0.37000 |
| 57 | 0.11750 | 0.05750 | 0.03500 | 0.003369 | 0.002800 | 0.05000 | 0.35000 |
| 58 | 0.12000 | 0.06000 | 0.03500 | 0.003684 | 0.003600 | 0.05000 | 0.33000 |
| 59 | 0.12000 | 0.06000 | 0.03500 | 0.004046 | 0.004400 | 0.05000 | 0.34000 |
| 60 | 0.12000 | 0.06000 |  | 0.004441 |  | 0.20000 | 0.34000 |
| 61 | 0.13000 | 0.06000 |  | 0.004876 |  | 0.18000 | 0.30000 |
| 62 | 0.13000 | 0.06000 |  | 0.005361 |  | 0.25000 | 0.35000 |
| 63 | 0.15000 | 0.07500 |  | 0.005894 |  | 0.22000 | 0.28000 |
| 64 | 0.15000 | 0.07500 |  | 0.006475 |  | 0.22000 | 0.28000 |
| 65 | 0.15000 | 0.07500 |  | 0.007128 |  | 0.27000 | 0.27000 |
| 66 | 0.15000 | 0.07500 |  | 0.007838 |  | 0.32000 | 0.32000 |
| 67 | 0.15000 | 0.07500 |  | 0.008605 |  | 0.30000 | 0.30000 |
| 68 | 0.15000 | 0.07500 |  | 0.009438 |  | 0.30000 | 0.30000 |
| 69 | 0.15000 | 0.07500 |  | 0.010305 |  | 0.30000 | 0.30000 |
| 70 | 0.15000 | 0.07500 |  | 0.011229 |  | 0.30000 | 0.30000 |
| 71 | 0.15000 | 0.07500 |  | 0.012205 |  | 0.30000 | 0.30000 |
| 72 | 0.15000 | 0.07500 |  | 0.013226 |  | 0.30000 | 0.30000 |
| 73 | 0.15000 | 0.07500 |  | 0.014336 |  | 0.30000 | 0.30000 |
| 74 | 0.15000 | 0.07500 |  | 0.015516 |  | 0.30000 | 0.30000 |
| 75 | 0.00000 | 0.00000 |  | 0.017745 |  | 1.00000 | 1.00000 |

[^2]TABLE 2
RATES OF SEPARATION FROM ACTIVE SERVICE - FEMALES

| AGE | Rates of Withdrawal Service |  |  | Death* | Disability | Rates of Retirement |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0-4 | 5-9 | 10+ |  |  | < 30 years of service | $\begin{gathered} >=30 \text { years } \\ \text { of service*** } \end{gathered}$ |
| 19 | 0.28000 | 0.00000 | 0.00000 | 0.000138 | 0.000000 |  |  |
| 20 | 0.28000 | 0.00000 | 0.00000 | 0.000139 | 0.000000 |  |  |
| 21 | 0.28000 | 0.00000 | 0.00000 | 0.000130 | 0.000000 |  |  |
| 22 | 0.28000 | 0.00000 | 0.00000 | 0.000132 | 0.000000 |  |  |
| 23 | 0.13500 | 0.12000 | 0.00000 | 0.000122 | 0.000000 |  |  |
| 24 | 0.13500 | 0.12000 | 0.00000 | 0.000135 | 0.000000 |  |  |
| 25 | 0.13500 | 0.12000 | 0.00000 | 0.000148 | 0.000000 |  |  |
| 26 | 0.13500 | 0.12000 | 0.00000 | 0.000161 | 0.000000 |  |  |
| 27 | 0.13500 | 0.12000 | 0.00000 | 0.000174 | 0.000000 |  |  |
| 28 | 0.13500 | 0.10000 | 0.06000 | 0.000198 | 0.000000 |  |  |
| 29 | 0.13500 | 0.08000 | 0.06000 | 0.000211 | 0.000000 |  |  |
| 30 | 0.13500 | 0.07000 | 0.06000 | 0.000235 | 0.000000 |  |  |
| 31 | 0.13500 | 0.07000 | 0.05750 | 0.000247 | 0.000000 |  |  |
| 32 | 0.13500 | 0.07000 | 0.05500 | 0.000270 | 0.000000 |  |  |
| 33 | 0.13000 | 0.07000 | 0.05000 | 0.000292 | 0.000136 |  |  |
| 34 | 0.13000 | 0.07000 | 0.04000 | 0.000313 | 0.000144 |  |  |
| 35 | 0.13000 | 0.07000 | 0.04000 | 0.000345 | 0.000152 |  |  |
| 36 | 0.13000 | 0.06500 | 0.04000 | 0.000364 | 0.000160 |  |  |
| 37 | 0.13000 | 0.06500 | 0.04000 | 0.000392 | 0.000168 |  |  |
| 38 | 0.12000 | 0.06500 | 0.03000 | 0.000420 | 0.000216 |  |  |
| 39 | 0.12000 | 0.06500 | 0.03000 | 0.000457 | 0.000264 |  |  |
| 40 | 0.12000 | 0.06500 | 0.03000 | 0.000493 | 0.000312 | 0.02000 |  |
| 41 | 0.12000 | 0.06500 | 0.03000 | 0.000529 | 0.000336 | 0.02000 |  |
| 42 | 0.11000 | 0.06000 | 0.03000 | 0.000575 | 0.000360 | 0.02000 |  |
| 43 | 0.11000 | 0.06000 | 0.02500 | 0.000621 | 0.000470 | 0.02000 |  |
| 44 | 0.10750 | 0.06000 | 0.02500 | 0.000669 | 0.000560 | 0.02000 |  |
| 45 | 0.10750 | 0.06000 | 0.02500 | 0.000728 | 0.000650 | 0.02000 | 0.60000 |
| 46 | 0.10750 | 0.05500 | 0.02500 | 0.000790 | 0.000750 | 0.02000 | 0.60000 |
| 47 | 0.10750 | 0.05500 | 0.02500 | 0.000854 | 0.000900 | 0.02000 | 0.60000 |
| 48 | 0.10750 | 0.05500 | 0.03000 | 0.000932 | 0.001000 | 0.02000 | 0.60000 |
| 49 | 0.10750 | 0.05500 | 0.03000 | 0.001013 | 0.001200 | 0.02000 | 0.60000 |
| 50 | 0.10750 | 0.05500 | 0.03000 | 0.001107 | 0.001400 | 0.02750 | 0.50000 |
| 51 | 0.10750 | 0.05000 | 0.03000 | 0.001203 | 0.001800 | 0.02750 | 0.58000 |
| 52 | 0.10750 | 0.05000 | 0.03000 | 0.001312 | 0.002500 | 0.02750 | 0.48000 |
| 53 | 0.10750 | 0.05000 | 0.03000 | 0.001432 | 0.002900 | 0.02750 | 0.35000 |
| 54 | 0.10750 | 0.05000 | 0.03000 | 0.001550 | 0.003000 | 0.02750 | 0.35000 |
| 55 | 0.10750 | 0.05000 | 0.03000 | 0.001687 | 0.003400 | 0.05750 | 0.35000 |
| 56 | 0.10750 | 0.05000 | 0.03000 | 0.001831 | 0.003900 | 0.05750 | 0.35000 |
| 57 | 0.10750 | 0.05000 | 0.03000 | 0.001979 | 0.004500 | 0.05750 | 0.35000 |
| 58 | 0.11500 | 0.05500 | 0.03000 | 0.002153 | 0.005200 | 0.05750 | 0.35000 |
| 59 | 0.11500 | 0.05000 | 0.03000 | 0.002341 | 0.006000 | 0.05750 | 0.40000 |
| 60 | 0.11500 | 0.05500 |  | 0.002554 |  | 0.25000 | 0.40000 |
| 61 | 0.11500 | 0.05500 |  | 0.002781 |  | 0.25000 | 0.40000 |
| 62 | 0.11500 | 0.05500 |  | 0.003045 |  | 0.25000 | 0.43000 |
| 63 | 0.15000 | 0.07500 |  | 0.003335 |  | 0.25000 | 0.43000 |
| 64 | 0.15000 | 0.07500 |  | 0.003665 |  | 0.24000 | 0.43000 |
| 65 | 0.15000 | 0.07500 |  | 0.004047 |  | 0.32000 | 0.32000 |
| 66 | 0.15000 | 0.07500 |  | 0.004482 |  | 0.32000 | 0.32000 |
| 67 | 0.15000 | 0.07500 |  | 0.004983 |  | 0.32000 | 0.32000 |
| 68 | 0.15000 | 0.07500 |  | 0.005549 |  | 0.30000 | 0.30000 |
| 69 | 0.15000 | 0.07500 |  | 0.006214 |  | 0.30000 | 0.30000 |
| 70 | 0.15000 | 0.07500 |  | 0.007047 |  | 0.30000 | 0.30000 |
| 71 | 0.15000 | 0.07500 |  | 0.008020 |  | 0.30000 | 0.30000 |
| 72 | 0.15000 | 0.07500 |  | 0.009141 |  | 0.30000 | 0.30000 |
| 73 | 0.15000 | 0.07500 |  | 0.010432 |  | 0.30000 | 0.30000 |
| 74 | 0.15000 | 0.07500 |  | 0.011918 |  | 0.30000 | 0.30000 |
| 75 | 0.00000 | 0.00000 |  | 0.013697 |  | 1.00000 | 1.00000 |

[^3]**An additional $15 \%$ are assumed to retire at 30 years of service for ages between 50 and 61 .

TABLE 3
RATES OF SALARY INCREASES

| SERVICE | RATE |
| :---: | :---: |
| 0 | 1.0875 |
| 1 | 1.0725 |
| 2 | 1.0575 |
| 3 | 1.0525 |
| 4 | 1.0500 |
| 5 | 1.0500 |
| 6 | 1.0500 |
| 7 | 1.0425 |
| 8 | 1.0375 |
| 9 | 1.0375 |
| 10 | 1.0350 |
| 11 | 1.0350 |
| 12 | 1.0350 |
| 13 | 1.0350 |
| 14 | 1.0325 |
| 15 | 1.0325 |
| 16 | 1.0300 |
| 17 | 1.0300 |
| 18 | 1.0300 |
| 19 | 1.0300 |
| $20 \&$ Over | 1.0300 |

TABLE 4
RATES* OF MORTALITY FOR MEMBERS RETIRED ON ACCOUNT OF SERVICE AND BENEFICIARIES OF DECEASED MEMBERS

| AGE | MALES | FEMALES | AGE | MALES | FEMALES |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 19 | 0.000391 | 0.000138 | 71 | 0.016452 | 0.010588 |
| 20 | 0.000375 | 0.000139 | 72 | 0.018593 | 0.012050 |
| 21 | 0.000358 | 0.000130 | 73 | 0.021049 | 0.013734 |
| 22 | 0.000331 | 0.000132 | 74 | 0.023851 | 0.015676 |
| 23 | 0.000315 | 0.000122 | 75 | 0.027028 | 0.017905 |
| 24 | 0.000320 | 0.000135 | 76 | 0.030602 | 0.020444 |
| 25 | 0.000336 | 0.000148 | 77 | 0.034587 | 0.023292 |
| 26 | 0.000352 | 0.000161 | 78 | 0.039041 | 0.026513 |
| 27 | 0.000379 | 0.000174 | 79 | 0.044029 | 0.030157 |
| 28 | 0.000395 | 0.000198 | 80 | 0.049635 | 0.034310 |
| 29 | 0.000422 | 0.000211 | 81 | 0.055955 | 0.039061 |
| 30 | 0.000437 | 0.000235 | 82 | 0.063111 | 0.044527 |
| 31 | 0.000463 | 0.000247 | 83 | 0.071199 | 0.050773 |
| 32 | 0.000487 | 0.000270 | 84 | 0.080301 | 0.057872 |
| 33 | 0.000509 | 0.000292 | 85 | 0.090522 | 0.065905 |
| 34 | 0.000530 | 0.000313 | 86 | 0.101952 | 0.074915 |
| 35 | 0.000549 | 0.000345 | 87 | 0.114654 | 0.085016 |
| 36 | 0.000577 | 0.000364 | 88 | 0.128665 | 0.096302 |
| 37 | 0.000603 | 0.000392 | 89 | 0.143989 | 0.108863 |
| 38 | 0.000638 | 0.000420 | 90 | 0.160712 | 0.123050 |
| 39 | 0.000671 | 0.000457 | 91 | 0.178804 | 0.138920 |
| 40 | 0.000714 | 0.000493 | 92 | 0.198051 | 0.156483 |
| 41 | 0.000766 | 0.000529 | 93 | 0.218317 | 0.175520 |
| 42 | 0.000827 | 0.000575 | 94 | 0.239259 | 0.195812 |
| 43 | 0.000899 | 0.000621 | 95 | 0.261186 | 0.217258 |
| 44 | 0.000982 | 0.000669 | 96 | 0.283265 | 0.239427 |
| 45 | 0.001087 | 0.000728 | 97 | 0.305387 | 0.261930 |
| 46 | 0.001204 | 0.000790 | 98 | 0.327282 | 0.284517 |
| 47 | 0.001324 | 0.000854 | 99 | 0.348776 | 0.307135 |
| 48 | 0.001468 | 0.000932 | 100 | 0.369901 | 0.329688 |
| 49 | 0.001626 | 0.001013 | 101 | 0.390782 | 0.352255 |
| 50 | 0.001799 | 0.001107 | 102 | 0.411187 | 0.374737 |
| 51 | 0.001977 | 0.001203 | 103 | 0.431062 | 0.396818 |
| 52 | 0.002169 | 0.001312 | 104 | 0.450248 | 0.418408 |
| 53 | 0.002375 | 0.001432 | 105 | 0.468723 | 0.439379 |
| 54 | 0.005010 | 0.003843 | 106 | 0.486214 | 0.459442 |
| 55 | 0.005241 | 0.003901 | 107 | 0.502842 | 0.478519 |
| 56 | 0.005470 | 0.003936 | 108 | 0.518425 | 0.496626 |
| 57 | 0.005705 | 0.003980 | 109 | 0.526364 | 0.513594 |
| 58 | 0.005953 | 0.004023 | 110 | 0.527081 | 0.527799 |
| 59 | 0.006188 | 0.004067 | 111 | 0.527841 | 0.528348 |
| 60 | 0.006440 | 0.004136 | 112 | 0.528560 | 0.528899 |
| 61 | 0.006695 | 0.004230 | 113 | 0.529280 | 0.529449 |
| 62 | 0.006988 | 0.004363 | 114 | 0.530000 | 0.530000 |
| 63 | 0.007307 | 0.004537 | 115 | 0.530000 | 0.530000 |
| 64 | 0.007675 | 0.004785 | 116 | 0.530000 | 0.530000 |
| 65 | 0.008433 | 0.005260 | 117 | 0.530000 | 0.530000 |
| 66 | 0.009329 | 0.005831 | 118 | 0.530000 | 0.530000 |
| 67 | 0.010364 | 0.006519 | 119 | 1.000000 | 1.000000 |
| 68 | 0.011575 | 0.007325 | 120 | 1.000000 | 1.000000 |
| 69 | 0.012972 | 0.008252 |  |  |  |
| 70 | 0.014580 | 0.009329 |  |  |  |

[^4]TABLE 5
RATES* OF MORTALITY FOR MEMBERS RETIRED ON ACCOUNT OF DISABILITY

| AGE | MALES | FEMALES | AGE | MALES | FEMALES |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 19 | 0.004236 | 0.002467 | 71 | 0.048747 | 0.035962 |
| 20 | 0.004016 | 0.002306 | 72 | 0.051444 | 0.038439 |
| 21 | 0.003774 | 0.002107 | 73 | 0.054500 | 0.041221 |
| 22 | 0.003603 | 0.001957 | 74 | 0.057940 | 0.044350 |
| 23 | 0.003495 | 0.001925 | 75 | 0.061798 | 0.047842 |
| 24 | 0.003504 | 0.001992 | 76 | 0.066103 | 0.051736 |
| 25 | 0.003736 | 0.002183 | 77 | 0.070900 | 0.056084 |
| 26 | 0.003971 | 0.002399 | 78 | 0.076232 | 0.060934 |
| 27 | 0.004219 | 0.002639 | 79 | 0.082143 | 0.066340 |
| 28 | 0.004488 | 0.002890 | 80 | 0.088648 | 0.072311 |
| 29 | 0.004752 | 0.003162 | 81 | 0.095770 | 0.078908 |
| 30 | 0.005021 | 0.003442 | 82 | 0.103505 | 0.086181 |
| 31 | 0.005289 | 0.003739 | 83 | 0.111836 | 0.094149 |
| 32 | 0.005568 | 0.004050 | 84 | 0.120744 | 0.102884 |
| 33 | 0.005851 | 0.004383 | 85 | 0.130223 | 0.112015 |
| 34 | 0.006147 | 0.004724 | 86 | 0.140302 | 0.121357 |
| 35 | 0.006444 | 0.005093 | 87 | 0.151074 | 0.130835 |
| 36 | 0.006773 | 0.005465 | 88 | 0.162552 | 0.140477 |
| 37 | 0.007132 | 0.005874 | 89 | 0.174851 | 0.150409 |
| 38 | 0.007522 | 0.006341 | 90 | 0.188001 | 0.160832 |
| 39 | 0.007955 | 0.006845 | 91 | 0.203357 | 0.171904 |
| 40 | 0.008444 | 0.007386 | 92 | 0.219659 | 0.183906 |
| 41 | 0.008995 | 0.007974 | 93 | 0.236102 | 0.197016 |
| 42 | 0.009624 | 0.008622 | 94 | 0.252755 | 0.211465 |
| 43 | 0.010357 | 0.009338 | 95 | 0.270439 | 0.227586 |
| 44 | 0.011191 | 0.010133 | 96 | 0.288744 | 0.245346 |
| 45 | 0.012146 | 0.011004 | 97 | 0.307955 | 0.264627 |
| 46 | 0.013230 | 0.011970 | 98 | 0.328018 | 0.285278 |
| 47 | 0.014450 | 0.013039 | 99 | 0.348776 | 0.307135 |
| 48 | 0.015800 | 0.014215 | 100 | 0.369901 | 0.329688 |
| 49 | 0.017278 | 0.015493 | 101 | 0.390782 | 0.352255 |
| 50 | 0.018432 | 0.016181 | 102 | 0.411187 | 0.374737 |
| 51 | 0.019644 | 0.016900 | 103 | 0.431062 | 0.396818 |
| 52 | 0.020912 | 0.017639 | 104 | 0.450248 | 0.418408 |
| 53 | 0.022201 | 0.018354 | 105 | 0.468723 | 0.439379 |
| 54 | 0.023502 | 0.019018 | 106 | 0.486214 | 0.459442 |
| 55 | 0.024790 | 0.019679 | 107 | 0.502842 | 0.478519 |
| 56 | 0.026023 | 0.020328 | 108 | 0.518425 | 0.496626 |
| 57 | 0.027200 | 0.020919 | 109 | 0.526364 | 0.513594 |
| 58 | 0.028337 | 0.021476 | 110 | 0.527081 | 0.527799 |
| 59 | 0.029446 | 0.022010 | 111 | 0.527841 | 0.528348 |
| 60 | 0.030569 | 0.022548 | 112 | 0.528560 | 0.528899 |
| 61 | 0.031731 | 0.023104 | 113 | 0.529280 | 0.529449 |
| 62 | 0.032970 | 0.023730 | 114 | 0.530000 | 0.530000 |
| 63 | 0.034292 | 0.024425 | 115 | 0.530000 | 0.530000 |
| 64 | 0.035689 | 0.025227 | 116 | 0.530000 | 0.530000 |
| 65 | 0.037177 | 0.026170 | 117 | 0.530000 | 0.530000 |
| 66 | 0.038753 | 0.027278 | 118 | 0.530000 | 0.530000 |
| 67 | 0.040426 | 0.028573 | 119 | 1.000000 | 1.000000 |
| 68 | 0.042220 | 0.030066 | 120 | 1.000000 | 1.000000 |
| 69 | 0.044172 | 0.031786 |  |  |  |
| 70 | 0.046328 | 0.033740 |  |  |  |

*Rates as of 2015


[^0]:    *An additional $10 \%$ are assumed to retire at 30 years of service for ages between 50 and 64 .
    ** An additional $15 \%$ are assumed to retire at 30 years of service for ages between 50 and 61 .

[^1]:    *Rates as of 2015

[^2]:    *Rates as of 2015
    **An additional $10 \%$ are assumed to retire at 30 years of service for ages between 50 and 64 .

[^3]:    *Rates as of 2015

[^4]:    *Rates as of 2015

